

**Source:** Troubleshooting Electronic Circuits: A Guide to Learning Analog Electronics, 1st Edition

**ISBN:** 9781260143560

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## 8. Troubleshooting Discrete Circuits (Simple Transistor Amplifiers)



Click [here](#) for the **Basic Amplifier Calculations SI units** spreadsheet calculator.

For this chapter we will be introducing transistor amplifiers that are “derived” from the LED circuits from [Chapter 7](#). We shall be showing that these amplifiers have limitations such as amplitude gain (ratio of output signal to input signal amplitudes), waveform distortion (e.g., a sine wave input signal with a distorted waveform at the output), output swing, and output current. In general, an amplifier is a circuit that provides a larger voltage signal or larger current signal at the output when compared to the input signal. All amplifier circuits require some type of supply voltage such as a 9-volt battery or a 12-volt power supply.

## 8.1. Important Practical Transistor Specifications

It should be noted that amplifiers are imperfect in that they cannot supply infinite current nor infinite voltage at their outputs. The transistors themselves have limitations on maximum collector-to-emitter voltage and maximum collector current, along with maximum power dissipation. For example, the ubiquitous 2N3904 NPN transistor has a typical maximum collector-to-emitter voltage ( $V_{CE}$ ) of 40 volts, a 200 mA maximum collector current ( $I_C$ ), and a 200 mW power dissipation rating. Power dissipation is usually given by  $P_d = V_{CE} \times I_C$ . For example in [Figure 8-1](#), suppose the collector current driving the light-emitting diode LED1 is **20 mA =  $I_C$** , and we have 9 volts as the supply BT2 with a red LED1 with a 2-volt forward turn-on voltage =  $V_F$ .  $BT2 = 9$  volts and  $V_F = 2$  volts so  $BT2 = V_F + V_{CE}$ , and  $V_{CE} = BT2 - V_F$  or  $V_{CE} = 9$  volts - 2 volts, so:

$$V_{CE} = 7 \text{ volts}$$

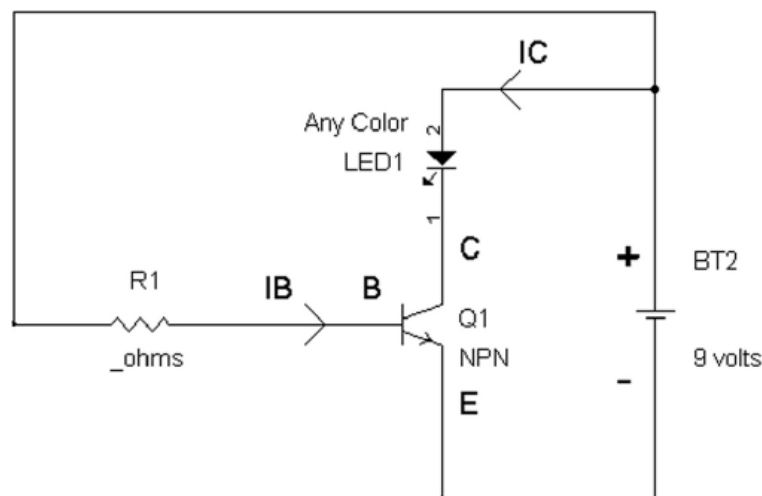
$$P_d = V_{CE} \times I_C, \text{ which is the power dissipation of transistor } Q1$$

$$P_d = 7 \text{ volts} \times 20 \text{ mA}$$

$$P_d = 140 \text{ mW}, \text{ which is fortunately below the } 200 \text{ mW} \text{ power dissipation rating of the } 2N3904$$

Although this example will work, as a rule of thumb, you want the power dissipation to be less than 50 percent of the maximum rating. In this example, the transistor is dissipating at 70 percent of maximum power dissipation (via  $140 \text{ mW} / 200 \text{ mW} = 70\%$ ), so we may want to use a higher wattage transistor, such as a 2N4401 where  $P_d = 500 \text{ mW}$  maximum.

**Figure 8-1** An LED drive circuit used for determining transistor Q1's power dissipation.



Note that both  $V_{CE} = 7$  volts and  $I_C = 20$  mA are well within the maximum specifications of 40 volts and 200 mA, respectively, for the 2N3904 transistor. However, this example shows that we have to keep track of power dissipation even if the voltages and currents are well within specifications.

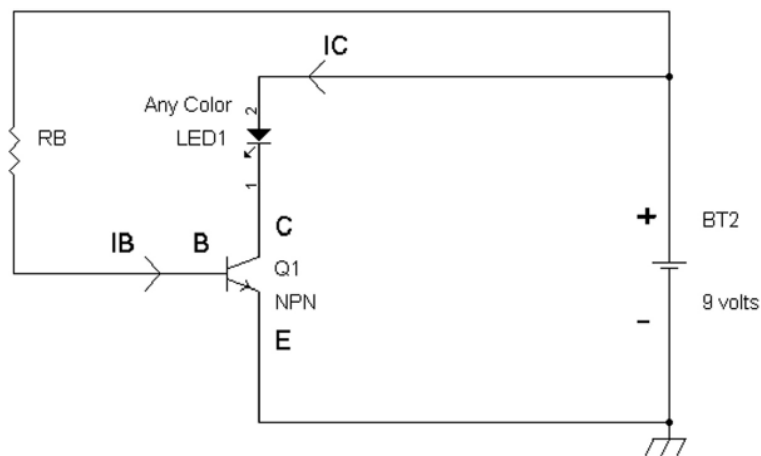
## 8.2. Simple Transistor Amplifier Circuits

The basic LED constant current source drive circuit shown in [Figure 8-2](#) can be reconfigured to operate as an amplifier as shown in [Figure 8-3](#).

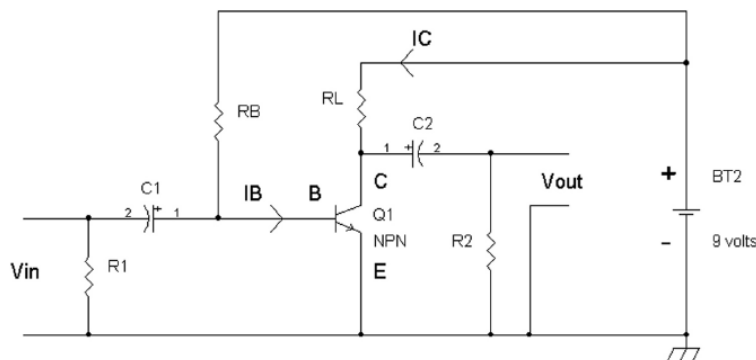
**Note:** The base driving resistor is renamed as  $R_B$ .

In [Figure 8-2](#) the transistor's base-to-emitter voltage is held constant via the base current driving resistor  $R_B$  that is connected to the power supply. With this constant base-to-emitter voltage, a constant collector current is provided to the LED. However, if we somehow are able to vary the base-to-emitter voltage by just a little, such as a variation of a few millivolts (mV), then the collector current will vary as well. See [Figure 8-3](#), which is essentially the same circuit with a couple of modifications.

**Figure 8-2** Constant current source to the LED via Q1's collector current.



**Figure 8-3** The constant current source LED drive circuit modified into an amplifier.



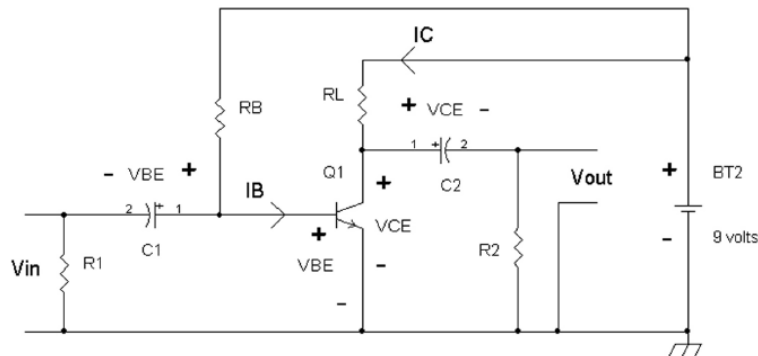
For this type of amplifier, the signals must be low level like the types of signals from microphones that produce  $< 10$  mV to avoid distorted output signals. If larger signals are used such as an audio signal from your digital or CD player, then the input should be attenuated with a voltage divider circuit. Typical attenuation would lower the amplitude by 10 to 100 fold.

Although this circuit is “easy” to analyze, it has limited purposes on its own as an amplifier. However, some circuits do not require low distortion. This circuit can be used for a fuzz pedal distortion amplifier used in an electric guitar, or be used in an oscillator circuit, or be used as a mixer that deliberately generates distortion products, such as in an RF mixer.

## 8.3. First DC Analysis: Capacitors = Batteries with Self Adjusting Voltages

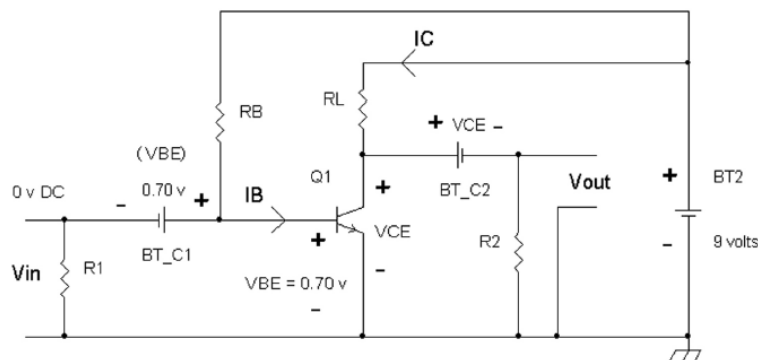
Capacitors C1 and C2 can be viewed as “fast charge” batteries that charge to a voltage such that no DC current flows through them. Let’s take a closer look at the one-transistor amplifier with some voltages labeled. See [Figure 8-4](#) first.

**Figure 8-4** Capacitors C1 and C2 are charged to voltages “VBE” and “VCE” as marked.



When we look at [Figure 8-5](#), the DC voltage at  $V_{in}$  is equal to the series voltages of  $BT\_C1$  and the voltage at the base-emitter junction of  $Q1$ . Because the polarities of  $BT\_C1$  and  $V_{BE}$  are the same with equal voltages via the + side of  $BT\_C1$  connected to the + side of  $V_{BE}$ , the voltage at  $V_{in}$  is 0 volts DC. This amounts to two back-to-back equal voltage sources connected in series such that the net voltage is zero. Here is another way to look at this. Suppose you have a two-cell flashlight. Instead of installing the 1.5-volt batteries correctly (in series) to provide 3 volts, you install them back to back, which gives zero volts instead.

**Figure 8-5** Batteries  $BT\_C1$  and  $BT\_C2$  can be thought of as replacing  $C1$  and  $C2$  as voltage sources.



In the amplifier, if the  $V_{BE}$  of  $Q1 = 0.70$  volts, capacitor  $C1$  charges up to exactly 0.70 volts in [Figure 8-4](#). In [Figure 8-5](#), we see if  $BT\_C1$  is 0.70 volt as labeled, then the DC voltage at  $V_{in}$  has to be zero volts due to series connection of back-to-back  $V_{BE}$  voltages from the  $Q1$  and  $C1$ .

Likewise, if  $C2$  in [Figure 8-4](#) is charged up to a voltage of  $V_{CE}$ , we see in [Figure 8-5](#) that the DC voltage at  $V_{out}$  has to be zero volts. The reason is that  $BT\_C2$  has an equal and opposing voltage to  $V_{CE}$ , the voltage at the collector of  $Q1$ . Thus, the DC voltage at  $V_{out}$  has to be zero volts due to the back-to-back series connection of  $V_{CE}$  from the transistor and  $V_{CE}$  in  $C2$  or  $BT\_C2$ .

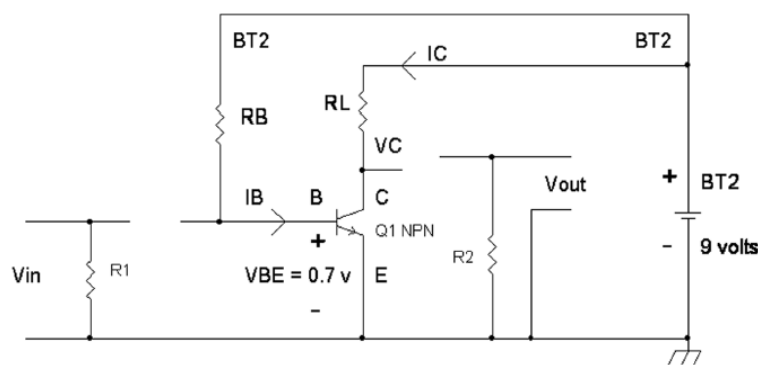
The capacitors C1 and C2 play two important roles. First, they block out DC currents from  $V_{in}$  and  $V_{out}$ . Second, they pass through an AC signal such as an audio signal.

## 8.4. Second DC Analysis: Take Out the Capacitors to Find the DC Currents and DC Voltages

With the capacitors removed we can now more clearly see for DC analysis. Not only the capacitors C1 and C2 have been removed but the adjoining components R1 and R2 are now also no longer part of the circuit. What we are left with is just three components,  $R_L$ ,  $R_2$ , and Q1, plus the power supply, BT2.

There are two reasons for determining the DC base and collector currents,  $I_B$  and  $I_C$ . Finding the expected base and collector currents will allow us to determine the collector-to-emitter voltage, which has to be  $> 0.7$  volts in most cases. For example, if the collector current is too high or the voltage drop across  $R_L$  is too high, then the transistor is in the saturation region, and the circuit will not amplify.

**Figure 8-6** To calculate the DC currents and voltages, remove all capacitors that are C1 and C2.



To determine the collector current  $I_C$ , first, we calculate for the base current  $I_B$ .

$$I_B = (BT2 - V_{BE})/R_B$$

For most good approximations,  $V_{BE} = 0.7$  volt.

$$I_B = (BT2 - 0.7 \text{ v})/R_B$$

$$I_B = \frac{(BT2 - 0.7 \text{ v})}{R_B}$$

Let's take some examples pertaining to [Figures 8-4](#) or [8-6](#):

If  $BT2 = 9$  volts and  $R_B = 56\text{k}\Omega$ , then  $I_B = (9 \text{ v} - 0.7 \text{ v})/56\text{k}\Omega = (8.3 \text{ v})/56\text{k}\Omega$

$$I_B = 0.148 \text{ mA or } I_B = 148 \mu\text{A}$$

$$I_C = \beta I_B$$

For this example, we use a lower current gain transistor such as a 2N3903 where  $\beta = 50$ . Since we already calculated the base current as  $I_B = 0.148 \text{ mA}$  then:

$$I_C = \beta I_B = 50 \times 0.148 \text{ mA}$$

$$I_C = 7.4 \text{ mA}$$

If we have  $R_L = 1000\Omega$ , then we can now find  $V_C$ , Q1's collector voltage reference to ground.

$$V_C = B T_2 - I_C (R_L)$$

$$V_C = 9 \text{ v} - 7.4 \text{ mA} (1000\Omega) = 9 \text{ v} - 7.4 \text{ v}$$

$$V_C = 1.6 \text{ volts}$$

What happens if  $\beta \rightarrow 100$ ?

$$\text{Then } I_C = \beta I_B = 100 \times 0.148 \text{ mA} = 14.8 \text{ mA.}$$

$$\text{We find that } V_C = 9 \text{ v} - 14.8 \text{ mA} (1000\Omega) = 9 \text{ v} - 14.8 \text{ v} = -5.8 \text{ volts} = V_C???$$

This is not possible since we only have a positive power supply and thus no negative volts can be generated. Instead,  $V_C \sim 0$  volts, and usually  $V_C \sim 0.2$  volt. That is, if the calculated value for  $V_C$  is  $< 0.5$  volt, usually the amplifier will not work because the transistor is now a switch that “shorts” the collector terminal to ground.

What we have shown in this example is that if the current gain is too high, the transistor amplifier in [Figure 8-4](#) can cause the transistor to turn into a switch. That is why a circuit like [Figure 8-4](#) requires selecting the  $\beta$  of transistors in a narrow range, such as  $30 < \beta < 50$ , or “tweaking” the resistance value of the base driving resistor,  $R_B$ .

For example, if we want to use a transistor whose  $\beta = 100$ , then we should approximately double the value of  $R_B$  from  $56\text{k}\Omega$  to  $110\text{k}\Omega$  with  $B T_2 = 9 \text{ v}$  and  $R_L = 1000\Omega$ . This leads to:

$$I_B = (B T_2 - 0.7 \text{ v}) / R_B = (9 \text{ v} - 0.7 \text{ v}) / 110\text{k}\Omega = 8.3 \text{ v} / 110\text{k}\Omega = 75.455 \mu\text{A}$$

$$I_C = 100 \times 75.455 \mu\text{A} = 7.545 \text{ mA}$$

$$V_C = B T_2 - I_C R_L = 9 \text{ v} - 7.545 \text{ mA} \times 1000\Omega = 9 \text{ v} - 7.545 \text{ v} = V_C$$

$V_C \sim 1.45$  volts, which is pretty close to  $V_C = 1.6$  volts for  $R_B = 56\text{k}\Omega$  and  $\beta = 50$ .

It would be safer to aim for a slightly higher  $V_C$ . We can have  $R_B = 120\text{k}\Omega$  with  $\beta = 100$  and  $R_L = 1000\Omega$ , which results in  $I_B = 69.167 \mu\text{A}$  and  $I_C = 100 \times 69.167 \mu\text{A}$  or  $I_C = 6.9167 \text{ mA}$ .

$$V_C = 9 \text{ v} - 6.9167 \text{ mA} \times 1000\Omega = 9 \text{ v} - 6.9167 \text{ v} = V_C$$

$$V_C = 2.08 \text{ v}$$

In the real world, the specific transistor part number (e.g., 2N3904, 2N2222, etc.) will not only have a range of  $\beta$ , but the current gain  $\beta$  will change with temperature. So, the DC collector current and DC collector voltage will vary. In general, the transistor amplifier in [Figure 8-4](#) is more of a hobbyist or DIY (do-it-yourself) amplifier where you have to individually tweak it to a desired collector current. We will find in the next section that the DC collector current  $I_C$  also determines the AC signal's gain at  $V_{out}$ , and also the input loading resistance at  $V_{in}$ .

For now, we have:

$$V_C = B T_2 - I_C (R_L)$$

$$I_C = \beta \frac{(B T_2 - 0.7 \text{ v})}{R_B}$$

A more general formula would be:

$$V_C = B T_2 - \beta \frac{(B T_2 - 0.7 \text{ v})}{R_B} (R_L)$$

For a current gain  $\beta = 50$ ,  $B T_2 = 9$  volts,  $R_B = 56\text{k}\Omega$  or  $56,000\Omega$ , and  $R_L = 1000\Omega$ .

$$V_C = 9\text{ v} - 50 \frac{(9\text{ v} - 0.7\text{ v})(1000)}{R_B} = 9\text{ v} - 7.4\text{ v} = V_C$$

$$V_C = 1.6\text{ volts}$$

And note the collector current:

$$I_C = \beta \frac{(V_{T2} - 0.7\text{ v})}{R_B} = 50 \times 0.148\text{ }\mu\text{A} = 7.4\text{ mA} = I_C$$

Alternatively, instead of using the general formula for  $V_C$ , sometimes it's more logical to find the base current,  $I_B$ , first and then calculate the collector current,  $I_C$  to find  $V_C$ , the collector voltage.

If  $V_{T2} = 5\text{ volts}$  and  $R_B = 100\text{k}\Omega$ , then  $I_B = (5\text{ v} - 0.7\text{ v})/100\text{k}\Omega = (4.3\text{ v})/100\text{k}\Omega$ .

$$I_B = 0.043\text{ mA or } I_B = 43\text{ }\mu\text{A}$$

If  $\beta = 78$ , then  $I_C = \beta I_B = 78 (43\text{ }\mu\text{A})$ .

$$I_C = 3.225\text{ mA}$$

Let  $R_L = 820\Omega$

$$V_C = V_{T2} - I_C (R_L) = 5\text{ volts} - 3.225\text{ mA} (820\Omega) = 5\text{ volts} - 2.6445\text{ volts} = V_C$$

$$V_C = 2.3555\text{ volts}$$

## 8.5. Finding the AC Signal Gain

The DC collector current is the most important DC characteristic to find for calculating the AC signal gain. Via the DC collector current we can also calculate the input resistance.

Input resistance to an amplifier is important since the input signal source itself usually has an output source resistance or an optimum input load resistance. For example, an antenna may have a  $50\Omega$  source resistance. To achieve maximum power transfer, the input resistance of the amplifier should be  $50\Omega$  as well.

In another example, if your signal source is a dynamic microphone, then the input resistance should be typically  $1000\Omega$  or more. If you should connect the dynamic microphone to an amplifier with a  $50\Omega$  input resistance, then you will lose signal amplitude from the microphone.

Thus, we have to keep in mind the amplifier's input resistance based on the application (e.g., RF amplifier, microphone preamplifier, sensor amplifier, etc.). This is particularly important when we have one amplifier's output connected to the input of a second amplifier.

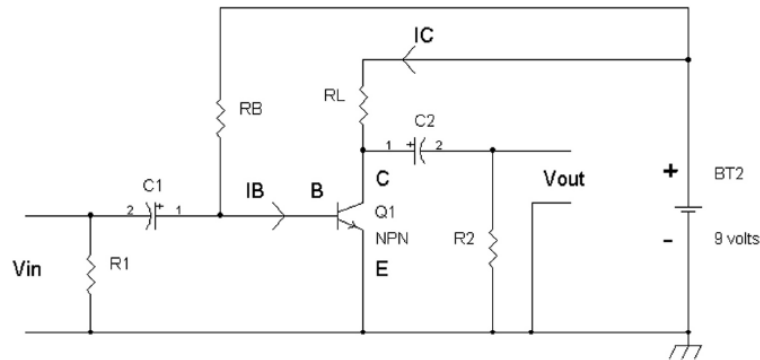
We can find the AC signal gain of this amplifier by noting the following:

- Capacitors with "sufficiently large" capacitances to be like batteries are AC short circuits or zero ohm resistors for AC signals.
- Power supplies are also treated as AC short circuits or zero ohm ( $0\Omega$ ) resistors with respect to AC signals.

At first glance, the second item may seem absurd. But if you think about it, if you probe for AC signals in a clean power supply or battery, you will find no AC signal. By definition, power supplies and batteries are DC voltage sources and thus cannot include any AC signal.

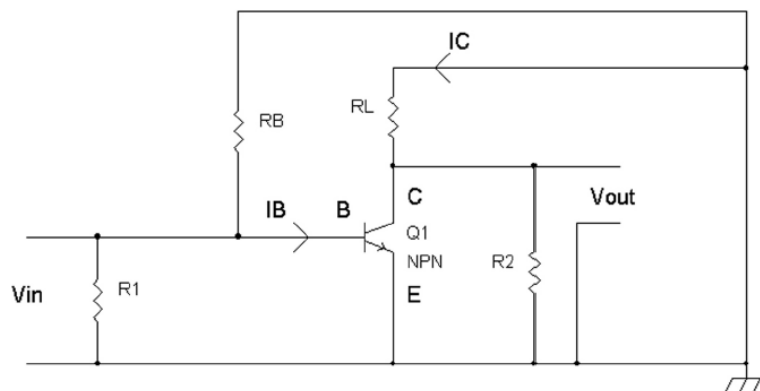
Likewise, if a capacitor has a large enough capacitance that it acts like a “battery” (e.g., see [Figure 8-5](#) again), then again by definition a battery cannot include an AC signal; it only produces a DC voltage. Let's take a look again at the “original” schematic in [Figure 8-7](#).

**Figure 8-7** The one-transistor amplifier from [Figure 8-5](#).



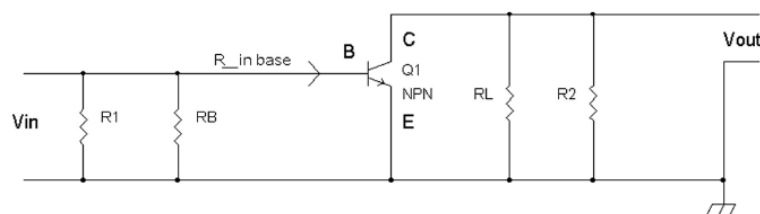
Now let's take a look at the AC analysis model shown in [Figure 8-8](#).

**Figure 8-8** The capacitors C1, C2, and battery (DC power supply) BT2 are “modeled” as AC short circuits or AC zero ohm wires.



[Figure 8-8](#) can be further redrawn to look simpler or more intuitively familiar. See [Figure 8-9](#).

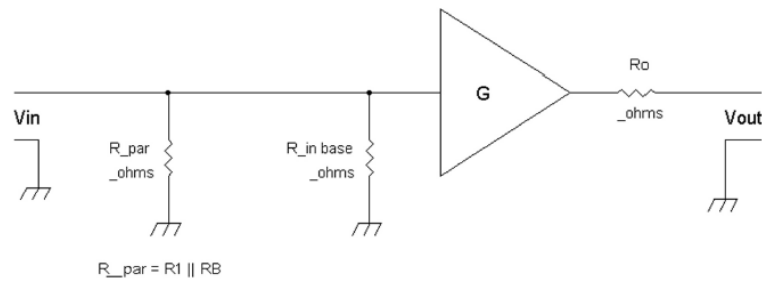
**Figure 8-9** A redrawn version of [Figure 8-8](#) to show a more intuitive idea of the one-transistor amplifier's AC analysis circuit.



As you can see in [Figure 8-9](#), the circuit looks a little “funny” in that there is no power supply. However, the schematic gives us an idea of how the AC signal at  $V_{in}$  will be amplified. Note that there is a resistance into Q1's base, which is referenced to ground.

Finally, we can model [Figure 8-9](#) in terms of a block diagram with the resistors  $R_1$ ,  $R_B$ ,  $R_L$ , and  $R_2$ . See [Figure 8-10](#). Note that  $R_{in\ base}$  is now “modeled” as a resistor to ground along with  $R_1$  and  $R_B$ .

Figure 8-10 A block diagram of Figure 8-9's AC analysis circuit.



In order to complete the AC analysis circuit, we have to find two “unknowns,” resistor,  $R_{\text{in base}}$ , and the gain, “G.” See below for the formulas given that  $I_C$  = DC collector current.

$$R_{\text{in base}} = \beta(0.026 \text{ v}/I_C)$$

$$G = -(I_C/0.026 \text{ v}) \times R_L \parallel R_2$$

$$\text{Where } R_L \parallel R_2 = \frac{R_L \times R_2}{R_L + R_2} = R_o \text{ and}$$

$$R_{\text{par}} = R1 \parallel RB = \frac{R1 \times RB}{R1 + RB}$$

Sometimes it is convenient to express the term  $(0.026 \text{ v}/I_C) = r_e$ , where a handy starting point of  $I_C = 1 \text{ mA}$  results in:

$$(0.026 \text{ v}/0.001 \text{ A}) = 26\Omega = r_e$$

From this 1 mA starting point we can find  $r_e$  for any other collector by a scaling factor such that  $r_e$  is inversely proportional to collector current. That is, for a given current:

$$r_e = \frac{0.001 \text{ A}}{I_C} \times 26\Omega$$

Since we often set collector currents in milliamps, mA, you can express the formula this way where the collector current  $I_C$  is in milliamps.

$$r_e = \frac{0.001 \text{ A}}{I_C \text{ mA}} \times 26\Omega$$

$$\text{For example, if } I_C = 2 \text{ mA, then } r_e = \frac{1 \text{ mA}}{2 \text{ mA}} \times 26\Omega = 13\Omega$$

$$\text{And if } I_C = 0.1 \text{ mA} = 100 \mu\text{A, then } r_e = \frac{1 \text{ mA}}{0.1 \text{ mA}} \times 26\Omega = 260\Omega$$

For the input resistance  $R_{\text{in base}}$ :

$$R_{\text{in base}} = \beta (0.026 \text{ v}/I_C) = \beta r_e$$

**Note:**  $R_{\text{in base}}$  is inversely proportional to  $I_C$ . For example, if you decrease  $I_C$  by tenfold, then  $R_{\text{in base}}$  increases by tenfold.

$$\text{For example, if } \beta = 5100 \text{ and } I_C = 1 \text{ mA, then } r_e = \frac{1 \text{ mA}}{1 \text{ mA}} \times 26\Omega.$$

$$r_e = 26\Omega$$

$$R_{\text{in base}} = \beta r_e = 100 \times 26\Omega = 2.6\text{K}\Omega$$

If  $\beta = 5100$  and we have  $I_C = 0.1 \text{ mA}$ , then  $R_{in \text{ base}} = \beta r_e = 26 \text{ K}\Omega$ .

For the gain factor  $G$ :

$$G = -(I_C / 0.026 \text{ v}) \times R_L \parallel R_2$$

**Note:**  $G$  is proportional to the DC collector current  $I_C$ . So, if you increase  $I_C$  by tenfold (e.g.,  $0.1 \text{ mA}$  to  $1 \text{ mA}$ ), the gain,  $G$ , goes up by tenfold. And if you decrease  $I_C$  by tenfold,  $G$ , decreases by tenfold.

In this amplifier given current gain  $\beta$ , if you increase the DC collector current the input resistance to the base,  $R_{in \text{ base}}$ , decreases while the gain,  $G$ , increases.

A decreasing  $R_{in \text{ base}}$  can cause the input signal to be loaded down and thus attenuated when we increase the DC collector current  $I_C$ . One way to offset this is to pick a transistor that has a higher  $\beta$ . For example, a 2N3904 may have a typical  $\beta$  of 150, but a 2N5088 has higher typical  $\beta$  of 300. So, if you want to increase the collector current twofold but keep the same  $R_{in \text{ base}}$  resistance, you can select a transistor with twice the  $\beta$ . To keep the same DC collector current  $I_C$ , this also means that  $R_B$  would be increased about twofold in resistance because of the higher current gain (e.g., twice the  $\beta$ ).

Now let's take one of the previous examples concerning DC analysis:

$$V_{B2} = 5 \text{ volts}, R_B = 100 \text{ k}\Omega, \text{ then } I_B = (5 \text{ v} - 0.7 \text{ v}) / 100 \text{ k}\Omega = (4.3 \text{ v}) / 100 \text{ k}\Omega$$

$$I_B = 0.043 \text{ mA or } I_B = 43 \mu\text{A}$$

$$\text{If } \beta = 78, \text{ then } I_C = \beta I_B = 78 (43 \mu\text{A}) = 3.225 \text{ mA.}$$

$$I_C = 3.225 \text{ mA} = 0.003225 \text{ A}$$

$$R_L = 820 \Omega$$

$$R_1 = R_2 = 220 \text{ K}\Omega$$

Let  $C_1 = C_2 = 33 \mu\text{f}$  (with  $C_1$  and  $C_2$  rated at  $\geq 16 \text{ volts}$ ),  $R_L = 820 \Omega$ ,  $R_2 = 100 \text{ K}\Omega$ , with  $I_C = 0.003225 \text{ A}$ .

## 8.5.1. Gain Calculation

$$G = -(I_C / 0.026 \text{ v}) \times R_L \parallel R_2$$

$$G = -(0.003225 \text{ A} / 0.026 \text{ v}) \times 820 \Omega \parallel 100 \text{ K}\Omega = -(0.124 \text{ A/v}) \times \frac{820 \times 100 \text{ K}}{820 + 100 \text{ K}} \Omega$$

$$820 \Omega \parallel 100 \text{ K}\Omega = \frac{820 \times 100 \text{ K}}{820 + 100 \text{ K}} \Omega = 813 \Omega$$

**Note:** The units  $\text{A/v}$  or amps per volt has a unit of  $(1/\text{resistance})$  or  $1/\Omega$ .

$$G = -(0.124 \text{ A/v}) \times 813 \Omega = -100.85 = \frac{V_{out}}{V_{in}}$$

$$\frac{V_{out}}{V_{in}} = G = -100.8$$

The minus sign indicates an inverted AC signal, or a signal that is 180 degrees out of phase.

For example, if  $V_{in}$  is a  $1 \text{ mV}$  peak sinewave, then  $V_{out}$  provides an inverted sinewave at  $100.8 \text{ mV}$  peak.

## 8.5.2. Base Resistance, $R_{in}$ Base Calculation

$$R_{in \text{ base}} = \beta (0.026 \text{ v}/I_C) = 78 (0.026 \text{ v}/0.003225\text{A}) = 78 (8.06\Omega)$$

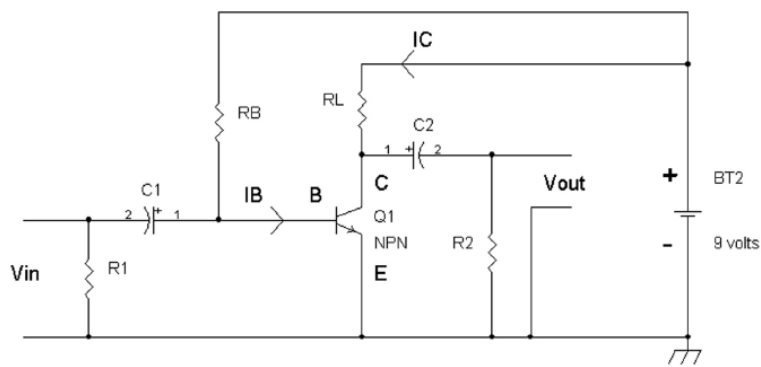
**Note** that the units v/A or volts per amp has a unit of resistance or  $\Omega$ .

$$R_{in \text{ base}} = 628.8\Omega$$

## 8.5.3. Limitations of This One-Transistor Amplifier

We will now look at the one transistor amplifier in terms of input amplitude range. See [Figure 8-11](#).

**Figure 8-11** The one-transistor amplifier that requires a low-level input signal to avoid distortion.



## 8.6. Limited Input Amplitude Range

When  $V_{in}$  is driven with a low-impedance generator such as one that has a  $50\Omega$  source resistance, which is common in many function generators, this amplifier will start to distort with signals starting at about 1-mV peak sine wave. For example, a 10-mV peak signal that is 20 mV peak to peak at the input will result in  $V_{out}$  having a generally larger amplitude but also a waveform that is distorted with about 10 percent second order harmonic distortion. As an example, if the frequency is 1000Hz, the output signal will provide a signal at 1000Hz, and another one at 2000Hz at 10 percent of the amplitude at 1000Hz.

Because this amplifier can produce so much distortion with signal sources from portable music players or smartphones (> 100 mV peak), you would need to place a voltage divider circuit such as a volume control to adjust the level into  $V_{in}$ , the input terminal.

See [Figure 8-12](#) for an amplifier with the following:

$$R_1 = 10\text{Meg}\Omega, R_2 = 10\text{Meg}\Omega, R_B = 4.7\text{Meg}\Omega, R_L = 12\text{K}\Omega, I_C = 0.3375 \text{ mA}$$

$$I_C = 0.0003375 \text{ A, or } I_C = 337.5 \mu\text{A}$$

$$Q_1 = 2\text{N}3904, BT = 9 \text{ volts}$$

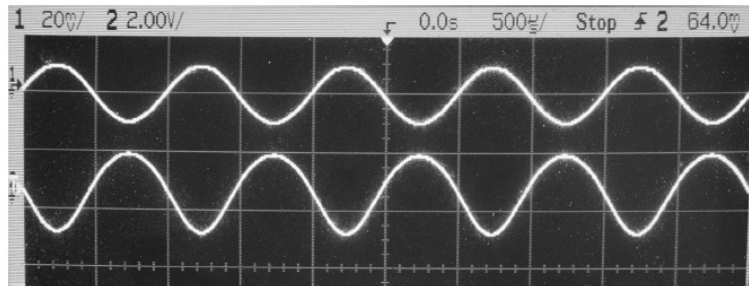
$G \sim -145$  as measured with 20 mV peak to peak sinewave at  $V_{in}$  with a  $50\Omega$  source resistance generator.

$G = -144$  as calculated. That is,  $G = -(0.0003375\text{A}/0.026 \text{ v}) 12\text{K}\Omega \sim -144$ .

**Note:**  $12\text{K}\Omega \parallel 10\text{Meg}\Omega = 12\text{K}\Omega$  within about 0.12%.

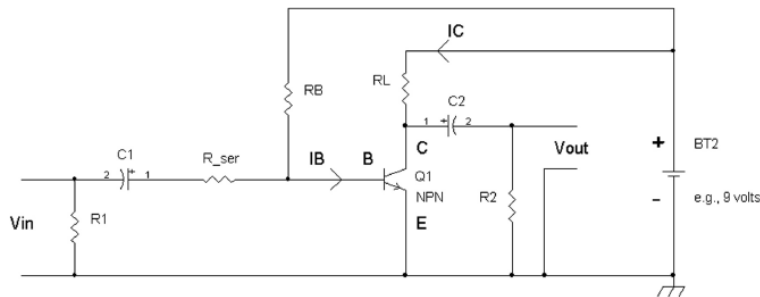
See below for the input and output signals.

**Figure 8-12** Amplifier 20 mV peak to peak signal input on top trace. Bottom trace shows a 2.7-volt peak to peak (inverted) output signal with 10 percent second harmonic distortion; and notice the rounder positive cycle and narrower negative cycle.



We can mitigate the distortion problem by using a series resistor,  $R_{ser}$ , as shown in [Figure 8-13](#).

**Figure 8-13** Lower distortion for the same output swing.



Typically, if we want lower distortion from an amplifier, we have to give up some of the voltage gain.

For example, if the gain of the amplifier is about 145, we can have lower distortion for the same output voltage if we set the series base resistor at about  $10 \times R_{in \text{ base}}$ . Again, if we use the previous example with:

$$R1 = 10\text{Meg}\Omega, R2 = 10\text{Meg}\Omega, R_B = 4.7\text{Meg}\Omega, R_L = 12\text{K}\Omega, I_C = 0.3375 \text{ mA or}$$

$$I_C = 337.5 \mu\text{A}$$

$$Q1 = 2\text{N}3904, BT = 9 \text{ volts}$$

$I_B$  is then calculated as about  $(9 \text{ v} - 0.7 \text{ v}) / 4.7\text{Meg}\Omega = 1.766 \mu\text{A}$ . We can now find  $\beta = I_C / I_B = (337.5 \mu\text{A} / 1.766 \mu\text{A})$ :

$$\beta = 191$$

This leads to  $R_{in \text{ base}} = \beta(0.026 \text{ v} / I_C)$  or  $R_{in \text{ base}} = 191(77\Omega)$ .

$R_{in \text{ base}} = 14.7\text{K}\Omega$ . If we make  $R_{ser}$  about  $10 \times R_{in \text{ base}}$ , then  $R_{ser} \sim 150\text{K}\Omega$ . The resulting distortion can now be compared with  $R_{ser} = 0 \Omega$  and  $R_{ser} = 150\text{K}\Omega$  for gain and distortion at  $V_{out}$  for the same output voltage. See [Table 8-1](#) that shows the effect on distortion with different values for input series resistor,  $R_{ser}$ . There is a trade-off in that you can have lower distortion but at the expense of lower voltage gain.

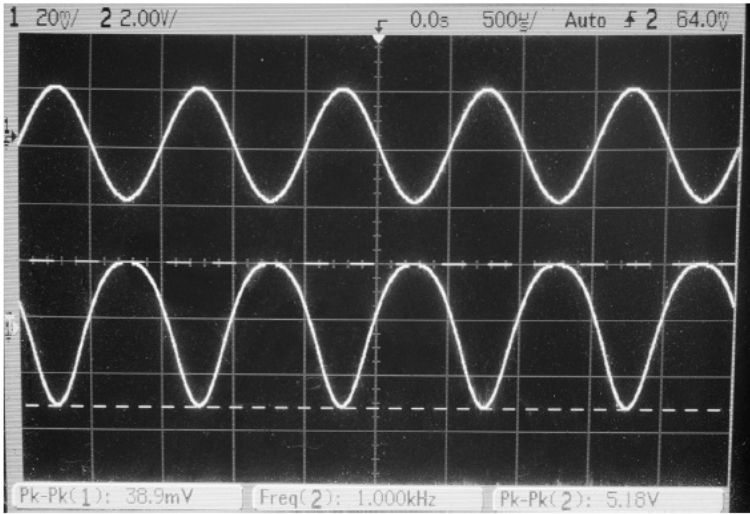
**Table 8-1** Distortion Measurements for the Same Amplitude Output at  $V_{out}$

$R_{ser}$	$V_{out}$ pk to pk	$V_{in}$ pk to pk	Gain	$V_{out}$ Distortion
$\sim 0 \Omega$	5.18 volts p-p	38.9 mV p-p	-133	$\sim 20\%$
150K $\Omega$	5.18 volts p-p	429 mV p-p	-12	$\sim 2\%$

**Note** that with the gain reduced by about tenfold, the distortion is reduced by  $\sim 10$  as well. Also it is preferred that  $R_B \gg R_{ser}$  for reducing distortion.

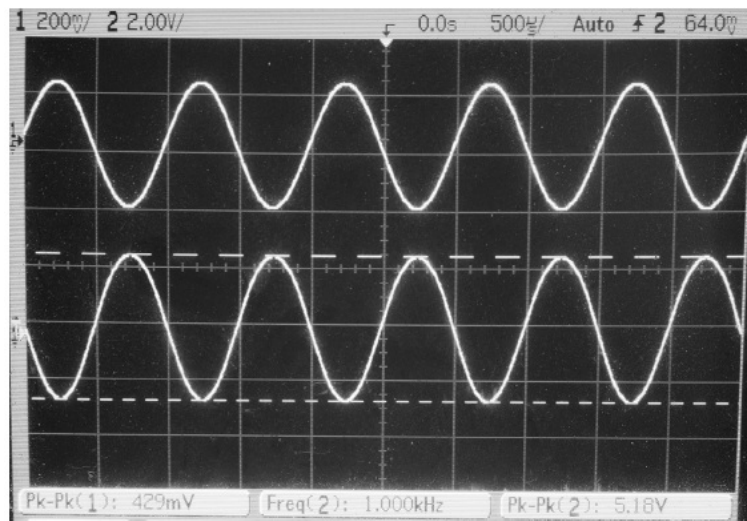
See [Figures 8-14](#) and [8-15](#), where the top trace waveforms are the input signals, and the bottom traces show the output signals. Note the phase inversions between output and input signals.

**Figure 8-14** Output waveform on the bottom trace with  $R_{ser} = \sim 0 \Omega$ , and note the compression on the positive cycle and narrowing on the negative cycle that denotes 20 percent harmonic distortion.



[Figure 8-15](#) shows when a “linearizing” series 150K resistor is added.

**Figure 8-15** Output waveform on bottom trace with  $R_{ser} = 150K\Omega$ , which shows almost no compression or narrowing distortion compared to [Figure 8-14](#). Harmonic distortion was measured at approximately 2 percent.



## 8.7. Output Swing Determined by $I_C$ and $R_L \parallel R_2$

To maximize output voltage swing, we should bias the collector current,  $I_C$ , such that the DC collector voltage is in a range of 40 to 60 percent of the supply voltage. For example, if the supply voltage such as BT2 in [Figure 8-13](#) is 10 volts (e.g., 8 AA rechargeable 1.25-volt batteries in series), then a good starting point will be at the 50 percent of 10 volts or = volts DC at the collector of Q1.  $R_B$  would be selected for this. The reason we want the DC collector voltage close to 50 percent of the supply voltage is to provide maximum output AC voltage swing. However, depending on the application, sometimes we just need a few volts of AC swing, peak to peak.

The maximum peak voltage swing without distortion is calculated as:

$V_{out \text{ max peak to peak}} = 2 \times I_C \times R_L \parallel R_5$ , where  $V_C \geq 50\%$  of power supply voltage

For example, suppose you have BT2 = 6 volts and  $R_L = 3K\Omega$ , and you bias  $R_B$  such that:

$I_C = 1 \text{ mA DC}$

This means that  $V_C = 6 \text{ volts} - I_C(R_L) = 6 \text{ volts} - 1 \text{ mA} (3K\Omega) = 6 \text{ volts} - 3 \text{ volts}$  or  $V_C = 3 \text{ volts}$ .

$V_C = 3 \text{ volts}$ , which is 50 percent of BT2 = 6 volts. This is a good starting point. If  $R_5$  is  $\gg R_L$ , such as  $R_L = 1 \text{ Meg}\Omega$ , then the output AC voltage swing will be close to 6 volts peak to peak.

This is because with  $R_5 \gg R_L$ ,  $R_L \parallel R_5 \sim R_L$ :

$V_{out \text{ max peak to peak}} = 2 \times I_C \times R_L \parallel R_5 \sim 2 \times I_C \times R_L = 2 \times 1 \text{ mA} \times 3K\Omega = 2 \times 3 \text{ volts}$

$V_{out \text{ max peak to peak}} \sim 6 \text{ volts peak to peak}$

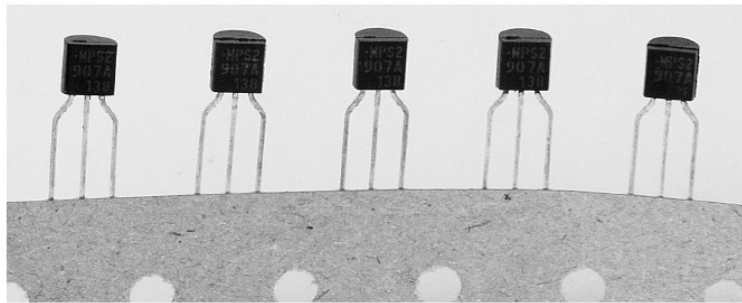
However, if  $R_5 = R_L$ , then  $R_L \parallel R_5 = 0.5 R_L$  and the voltage swing will be reduced by 50 percent. For example, when  $R_L = 3K\Omega$  and  $R_5 = 3K\Omega$ , the output voltage swing is reduced by 50 percent.

$$\begin{aligned}V_{out} \text{ max peak to peak} &= 2 \times I_C \times R_L || R_5 = 2 \times I_C \times R_L || R_L = \\2 \times I_C \times 0.5 R_L &= I_C \times R_L = V_{out} \text{ max peak to peak} \\V_{out} \text{ max peak to peak} &= 1 \text{ mA} \times 3\text{K}\Omega = 3 \text{ volts peak to peak}\end{aligned}$$

If the 3 volts peak to peak  $V_{out}$  max is sufficient, then you do not need to change the circuit. However, if  $R_5$  is lower in value such as  $2\text{K}\Omega$  or  $1\text{K}\Omega$  and you still want 3 volts peak to peak output, then you have to make  $R_L$  a smaller resistance such as lowering it to  $2\text{K}\Omega$  or  $1\text{K}\Omega$  while reselecting  $R_B$  to have  $V_C = 3$  volts DC such that the DC collector current,  $I_C$  is increased.

So far, the one-transistor amplifier circuits presented have many variables in terms of gain, input resistance, and DC operating points such as collector current  $I_C$  and collector voltage  $V_C$  due to the variation in  $\beta$ , the current gain. If you need to build many of these amplifiers and make them repeatable, you can buy the transistors in tape form as shown in [Figure 8-16](#). They should be reasonably matched in terms of turn-on voltage and  $\beta$ , but check them with a DVM for confirmation.

**Figure 8-16** Transistors on tape are reasonably matched for  $\beta$  and  $V_{BE}$  turn-on voltage.



### 8.7.1. Troubleshooting the One-Transistor Amplifier

The one-transistor amplifier may not work for the following reasons:

- If the transistor is put in backwards with the collector and emitter swapped, then the collector current will be very low because  $\beta \rightarrow 1$  or 2. This will result in very low gain since the collector current will be too small. So, expect  $V_C$  to be almost the same voltage as the power supply, which says that the voltage across  $R_L$  is close to zero volts.
- If the collector and emitter terminals are reversed, and the power supply voltage is  $> 6$  volts DC, there's a good chance that the transistor will act like a Zener diode, and the voltage at the collector will be in the range of  $\approx 7$  volts DC, but there will be very little signal output at  $V_{out}$ .
- If you replace the transistor, but find that the output signal is low, check the DC collector voltage,  $V_C$ . If the collector's voltage  $V_C$  is close to 0 volts (e.g.,  $< 0.5$  volt), the transistor is in saturation because there is too much base current. Reselect the base driving resistor,  $R_B$ , to have  $V_C$  at about half the supply voltage, or select a transistor with lower current gain,  $\beta$ . You may also have to confirm the proper resistance values for  $R_L$  and  $R_B$ . If  $R_L$  is too high in resistance and or if  $R_B$  is too low in resistance, it can cause the transistor to be in saturation.
- If you think you connected everything correctly but you find strange DC readings and output signals, make sure the transistor is the correct polarity (e.g., NPN or PNP). Sometimes it's easy to inadvertently put in the wrong polarity transistor and/or put it in with swapped leads.
- Check power supply voltage, and always add a bypass capacitor such as  $0.1 \mu\text{f}$  to  $1 \mu\text{f}$  across the power supply voltage source close to the transistor amplifier. Also note the supply voltage and choose the bypass capacitor to have at least twice the voltage rating. For example, if the supply voltage is 12 volts, choose a 25-volt to 100-volt capacitor.

## 8.8. Using Negative Feedback to Build “Mass Production” Amplifiers

If we look at the one-transistor amplifier schematic in [Figure 8-13](#) with its output waveform in [Figure 8-14](#), we will notice that the AC signal going into the base produces a signal at the collector that is in negative phase or opposite phase of the input.

This makes sense because the DC collector voltage,  $V_C = V_{CC} - I_C (R_L)$ . Since  $I_C$  is proportional to base current,  $I_B$ , and  $I_B$  is some function of the base voltage, then an increase in base current causes an increase in collector current. But an increase in collector current,  $I_C$ , causes a decrease in  $V_C$  due to  $V_C = V_{CC} - I_C (R_L)$ . For example, if  $V_{CC} = 10$  volts,  $R_L = 1\text{K}\Omega$ , then  $V_C = 5$  volts  $- I_C 1\text{K}\Omega$ . If we start out with  $I_C = 1$  mA, then  $V_C = 5$  volts  $- 1$  mA  $1\text{K}\Omega = 5$  volts  $- 1$  volt.

$$V_C = 4 \text{ volts}$$

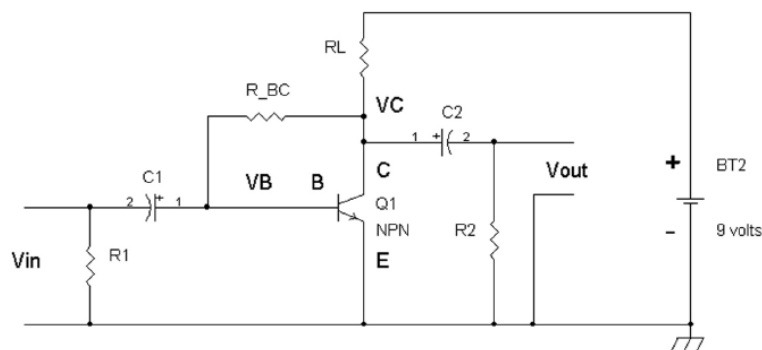
Suppose we increase the collector current such that  $I_C \rightarrow 3$  mA, then:

$$V_C = 5 \text{ volts} - 3 \text{ mA } 1\text{K}\Omega = 5 \text{ volts} - 3 \text{ volts} = 2 \text{ volts}$$

$$V_C = 2 \text{ volts}$$

As we can see, an increase in collector current results in a decrease in collector voltage. Since an increase in base current causes an increase in base voltage, then it follows that an increase in base voltage causes an increase in collector current, which causes a decrease in collector voltage. Thus, we have a “negative” phase relationship between the base and collector terminals. If we have this relationship, we can apply a self-biasing resistor between the base and collector as shown in [Figure 8-17](#). If this resistor is chosen properly, we can set a DC collector voltage and collector current that is not as sensitive to  $\beta$  variations. As long as  $\beta \gg 1$  such as  $\beta \geq 20$ , the DC collector current that is set by this circuit will not vary much whether the transistor has a  $\beta$  of 50 or a  $\beta$  of 500. Also, as long as the AC signal's gain is kept to  $\leq 10$ , the gain will be set by two resistors and it again will be insensitive to  $\beta$  variations.

**Figure 8-17** A simple self-biasing one-transistor amplifier via  $R_{BC}$  for “insensitivity” to  $\beta$ .

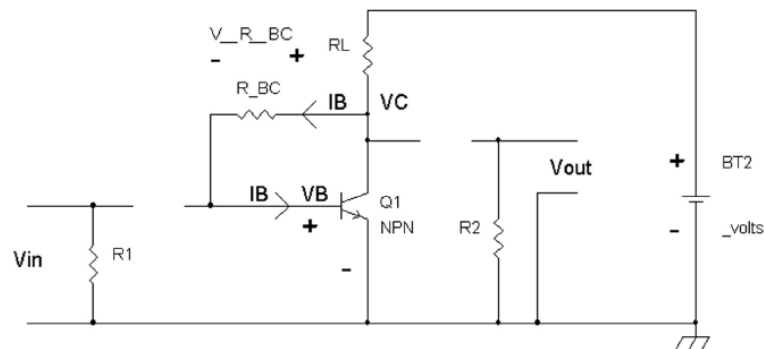


## 8.9. DC Analysis of Self-Biasing Amplifier

With a negative feedback resistor  $R_{BC}$  that is connected from the collector to base, a DC voltage is established at  $V_C$ . For the DC analysis, see [Figure 8-18](#).

Typically, the base-emitter voltage at  $V_B$  is  $\sim 0.7$  volt. If  $Q1$ 's  $\beta$  is greater than 50, then there's a good chance that  $Q1$ 's base current,  $I_B$ , is very small such that there is a very small voltage across  $R_{BC}$ ,  $V_{R_{BC}} = I_B \times R_{BC}$ . (Refer to [Figure 8-18](#).)

**Figure 8-18** DC analysis circuit for the self-biasing one-transistor amplifier via removing the DC blocking capacitors.



**Note** that  $V_C = V_{R\_BC} + V_B$  or  $V_C = (I_B \times R_{BC}) + V_B$ .

If this voltage across resistor  $R_{BC}$ ,  $V_{R\_BC} \ll 0.7$  volt, then  $V_C \sim V_B$ . A commonly used transistor, such as 2N4124 or equivalent, generally has  $\beta \geq 50$  at currents from 100  $\mu\text{A}$  to about 20 mA.

For power supply voltages that are  $\gg 0.7$  volts (e.g.,  $\geq$  volts) even with base current  $I_B$  flowing through  $R_{BC}$  in the order of  $V_{R\_BC} = 0.7$  volts such that  $V_C = 1.4$  volts versus  $V_C = 0.7$  volts, the collector current will vary  $< 25$  percent for  $BT2 \geq$  volts.

For example, with  $BT2 = 5$  volts,  $I_C \sim (BT2 - V_C)/R_L$

With  $V_C = 0.7$  volt,  $I_C \sim (5 \text{ volts} - 0.7 \text{ volt})/R_L$  or  $I_{C0.7V} \sim 4.3 \text{ volts}/R_L$ .

With  $V_C = 1.4$  volts,  $I_C \sim (5 \text{ volts} - 1.4 \text{ volts})/R_L$  or  $I_{C1.4V} \sim 3.6 \text{ volts}/R_L$ .

We can take the ratio of the two collector currents for  $V_C = 0.7$  volt and 1.4 volts to determine the change in collector current.

$(I_{C0.7V}/I_{C1.4V}) = [(4.3 \text{ volts}/R_L)/(3.6 \text{ volts}/R_L)]$ , the  $R_L$ 's cancel out, leaving  $(I_{C0.7V}/I_{C1.4V}) = (4.3 \text{ volts}/3.6 \text{ volts}) = 1.1944$ , which is a 19.44 percent change in collector current.

Let's take a look at some typical component values.  $Q1 = 2N4124$  or  $2N3904$ ,  $BT2 = 5$  volts,  $R_L = 3300\Omega$ ,  $R_{BC} = 100K\Omega$ , with  $\beta = 170$ , the measured  $V_C = 1.3$  volts. The collector current with  $\beta = 170$  is:

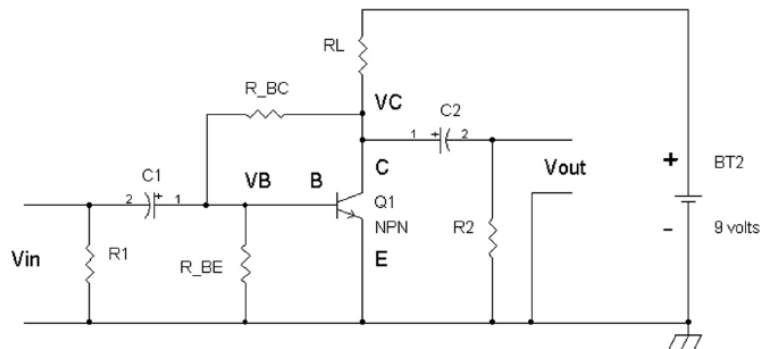
$$I_C \sim (5 \text{ volts} - 1.3 \text{ volts})/3300\Omega = 1.12 \text{ mA} = I_C$$

If we replace  $Q1$  with a 2N5089 where  $\beta = 461$ ,  $V_C = 0.9$  volt, and  $I_C = (5 \text{ volts} - 0.9 \text{ volts})/3300\Omega = 1.24 \text{ mA}$  for  $\beta = 461$ , which is only about a 10.8 percent change with 1.12 mA for  $\beta = 171$ . So even when  $\beta$  increased from 170 to 461, a 2.77-fold increase, the collector current,  $I_C$ , only increased by about 10.8 percent.

Having  $V_C$  biased at a DC voltage of about 1 volt will limit the voltage swing from about 0 volt to about 2 volts or 2 volts peak to peak before clipping of the output waveform occurs.

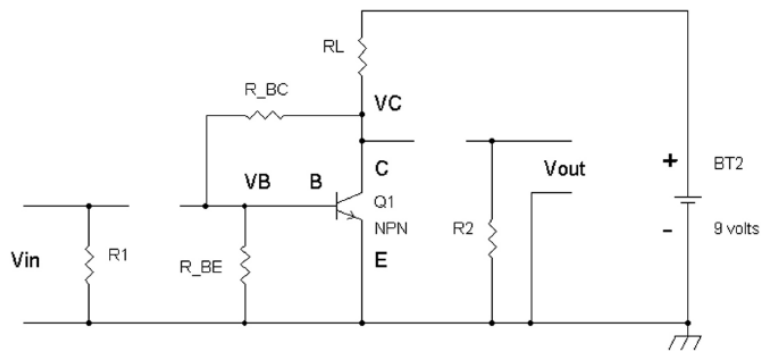
To maximize output voltage swing, it is generally better to have  $V_C$  set to about one half the supply voltage. For example, if  $BT2 = 5$  volts, and  $V_C$  is set to 2.5 volts DC, then the output swing can be from about 0 volts to nearly = volts, or close to = volts peak to peak. By adding a resistor ( $R_{BE}$ ) across the base-emitter terminals, we can raise  $V_C$ 's DC voltage. See [Figure 8-19](#).

**Figure 8-19** Adding an extra resistor  $R_{BE}$  to form a voltage divider with  $R_{BC}$ .



By adding  $R_{BE}$ , we can raise the DC collector voltage. See **Figure 8-20** for the DC analysis schematic.

**Figure 8-20** DC analysis circuit for **Figure 8-19**.



Since  $V_B \sim 0.7$  volt, we can work backwards to find  $V_C$  since the voltage across  $R_{BE}$  is  $\sim 0.7$  volt. By using a voltage divider formula and neglecting the base current from  $Q_1$ , we have:

$$0.7 \text{ volt} = V_B = V_C [R_{BE} / (R_{BE} + R_{BC})]$$

$$0.7 \text{ volt} / [R_{BE} / (R_{BE} + R_{BC})] = V_C$$

$$V_C = 0.7 \text{ volt} [(R_{BE} + R_{BC}) / R_{BE}]$$

In essence the DC voltage at the collector,  $V_C$ , is a scaled "up" voltage of  $V_{BE}$ .

For example, if we want  **$V_C = 1.4$  volts**, then  $R_{BC} = R_{BE}$ .

$$V_C = 0.7 \text{ volt} [(R_{BE} + R_{BE}) / R_{BE}] = 0.7 \text{ volt} [2R_{BE} / R_{BE}] = 0.7 \text{ volt} \times 2$$

$$V_C = 1.4 \text{ volts}$$

A general formula where it is easier to just find the ratio of  $R_{BC}$  to  $R_{BE}$  based on having a specified  $V_C$  is shown here:

$$R_{BC} / R_{BE} = (V_C / 0.7 \text{ v}) - 1$$

For example, if  $BT_2 = 5$  volts,  $R_L = 3300\Omega$ , and we want  $V_C = 2.5$  volts, then:

$$R_{BC} / R_{BE} = (2.5 / 0.7 \text{ v}) - 1 = 3.57 - 1 = 2.57$$

$$R_{BC} = 2.57 (R_{BE})$$

We can make  **$R_{BE} = 39K\Omega$**  so that  $R_{BC} = 2.57 (39K\Omega)$

$$R_{BC} = 100K\Omega$$

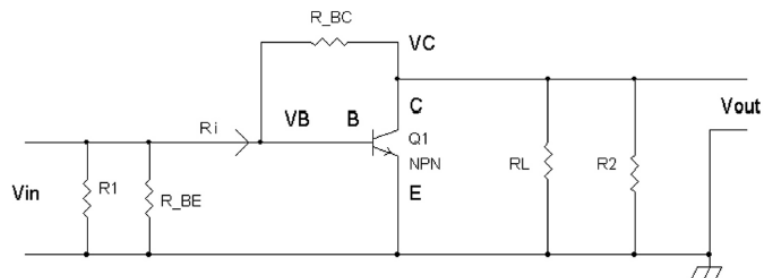
In general  $V_C$  will be a bit higher than calculated using a general-purpose transistor such as with a 2N4124 transistor. With a higher  $\beta$  transistor such as a 2N5089, the calculated  $V_C$  voltage will be closer in practice.

To preserve good voltage swing,  $R_{BC} \gg R_L$ . For example, if  $R_L = 1\text{K}\Omega$ ,  $R_{BC} \geq 10\text{K}\Omega$ . However, we will see that the simple 1 transistor amplifier has a “drawback” in terms of input resistance being too low. But not to worry—we use the lower input resistance to our advantage by adding a series input resistor to set the gain of the amplifier (see  $R_1$  in [Figure 8-25](#) if you are curious)..

## 8.10. AC Analysis of a Self-Biased Amplifier

Adding the feedback resistor  $R_{BC}$  causes a lower total input resistance as “seen” by  $V_{in}$  (see [Figure 8-21](#)).

**Figure 8-21** AC analysis circuit for the one-transistor feedback amplifier.



With negative feedback via the collector to base resistor,  $R_{BC}$ , this resistor and with the amplifier's gain,  $G$ , will result in a low-value resistor,  $R_i$ , referenced to ground, where  $R_i$  is in parallel with  $R_1$  and  $R_{BE}$ .

$R_i \sim [R_{BC}/(1 - G)] \parallel R_{in\text{ base}}$ , where  $G = V_{out}/V_{in}$ , and since this is an inverting amplifier,  $G$  will be a negative number.

$$G \sim - (I_C / 0.026 \text{ v}) \times (R_L \parallel R_2 \parallel R_{BC})$$

The gain,  $G$ , is calculated to be the same as the simple transistor amplifier shown in [Figure 8-10](#) when  $R_{BC} \gg R_L \parallel R_2$ . For a good enough approximation where  $R_{BC} \geq 10 \times (R_L \parallel R_2)$ , use:

$$G \sim - (I_C / 0.026 \text{ v}) \times (R_L \parallel R_2)$$

For example, if the supply voltage  $BT_2 = 12$  volts,  $Q_1 = 2N5089$  where  $\beta = 400$ ,  $R_L = 4700\Omega$ ,  $R_{BC} = 100\text{K}\Omega$ ,  $R_{BE} = 20\text{K}\Omega$  and  $V_B = 0.7$  volt, then  $V_C = 0.7 \text{ v} [(R_{BC}/R_{BE}) + 1]$ .

$$V_C = 0.7 \text{ volt} [(100\text{K}/20\text{K}) + 1] = 0.7 \text{ volt} [6]$$

$$V_C = 4.2 \text{ volts}$$

$$I_C \sim (BT_2 - V_C) / R_L = (12 \text{ volts} - 4.2 \text{ volts}) / 4700\Omega = 7.8 \text{ volts} / 4700\Omega$$

$$I_C \sim 1.66 \text{ mA} = 0.00166 \text{ A}$$

Let  $R_2 = 1\text{Meg}\Omega$  so that  $R_L \parallel R_2 = 4700\Omega \parallel 1\text{Meg}\Omega \sim 4700\Omega = R_L \parallel R_2$ .

$$G \sim - (I_C / 0.026 \text{ V}) \times (R_L \parallel R_2)$$

$$G \sim - (0.00166 \text{ A} / 0.026 \text{ V}) \times (4700 \Omega)$$

$$G \sim -300$$

$$R_{\text{in base}} = \beta(0.026 \text{ V} / I_C) = 400(0.026 \text{ V} / 0.00166 \text{ A})$$

$$R_{\text{in base}} = 6.26 \text{ K}\Omega = \text{internal resistance across the base and emitter of Q1}$$

$$R_i \sim [R_{BC} / (1 - G)] \parallel R_{\text{in base}}$$

$$R_i \sim [100 \text{ K}\Omega / (1 - -300)] \parallel 6.26 \text{ K}\Omega = [100 \text{ K}\Omega / (1 + 300)] \parallel 6.26 \text{ K}\Omega$$

$$R_i \sim 332 \Omega \parallel 6.26 \text{ K}\Omega$$

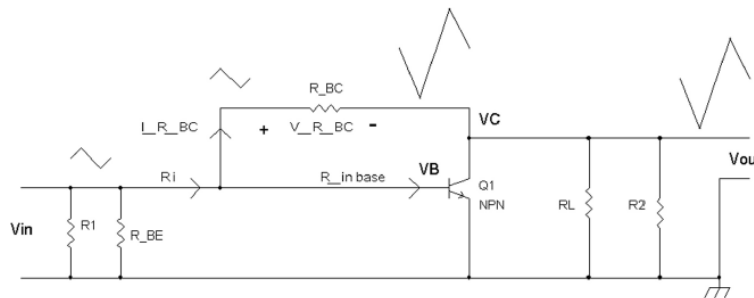
Since  $332 \Omega \ll 6.26 \text{ K}\Omega$ ,  $332 \Omega \parallel 6.26 \text{ K}\Omega \sim 332 \Omega$ , which leads to an approximation of:

$$R_i \sim 332 \Omega$$

$R_{\text{in base}}$  is the resistance into the base-emitter junction of the transistor that does not include any of the other external resistors such as  $R_{BC}$ ,  $R_{BE}$ , and  $R_1$ .

The resistance  $[R_{BC} / (1 - G)]$  is due entirely to  $V_{\text{in}}$ 's signal current flowing through  $R_{BC}$ , which results in a lower equivalent resistor,  $R_{BC} / (1 - G)$  referenced to ground. So, the question arises as to how we get such a lower equivalent resistor that is related to the amplifier's gain,  $G$ ? See [Figure 8-22](#).

**Figure 8-22** Input and output waveforms showing increased AC voltage across  $R_{BC}$ .



The amplifier produces an amplified (e.g., a larger amplitude) signal at the output,  $V_{\text{out}}$ , which is in opposite phase of the smaller amplitude input signal,  $V_{\text{in}}$ . This opposite phase signal at  $V_{\text{out}}$  then pulls extra current through the resistor  $R_{BC}$ . By pulling extra current, it makes it appear that  $V_{\text{in}}$  is driving an equivalently lower-value resistor that is referenced to ground like  $R_1$ .

An example of this lowered resistance effect is if we imagine that the gain,  $G = -1$  and  $R_{BC} = 1 \text{ K}\Omega$ , then what happens when  $V_{\text{in}} = 11 \text{ V}$ ? The output voltage is then  $-1 \text{ V}$  due to  $G = -1$ . However, the current flowing through the  $1 \text{ K}\Omega$  has a potential difference of  $11 \text{ V} - -1 \text{ V}$  or  $2 \text{ V}$ . This means the resistor current is now  $2 \text{ V} / 1 \text{ K}\Omega = 2 \text{ mA}$ . A  $11 \text{ V}$ -input across an equivalent resistor referenced to ground that will drain  $2 \text{ mA}$  would result in a  $500 \Omega$  resistor since  $1 \text{ V} / 500 \Omega = 2 \text{ mA}$ .

In general, the voltage across resistor  $R_{BC}$  is  $V_{R_{BC}}$ , which has  $V_{\text{in}}$  on one side and  $V_{\text{out}}$  on the other side. Thus,  $V_{R_{BC}} = V_{\text{in}} - V_{\text{out}}$ , but  $V_{\text{out}} = -G V_{\text{in}}$ , so:

$$V_{R_{BC}} = V_{\text{in}} - -G V_{\text{in}} = V_{\text{in}} + G V_{\text{in}}$$

$$V_{R_{BC}} = V_{\text{in}} (1 + G)$$

The current through  $R_{BC}$  is then:

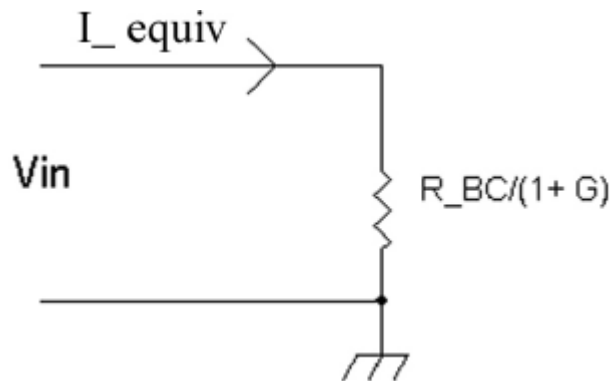
$$I_{R_{BC}} = V_{R_{BC}} / R_{BC}$$

and by substituting  $V_{in} (1 + G)$  for  $V_{R\_BC}$ :

$$I_{R\_BC} = V_{in} (1 + G) / R_{BC}$$

We want to now model an equivalent resistor referenced to ground (as shown in [Figure 8-23](#)) that will drain the same amount of current as  $I_{R\_BC}$ , which is  $I_{R\_BC} = I_{equiv} = V_{in} (1 + G) / R_{BC}$ .

**Figure 8-23** Equivalent resistor referenced to ground that drains the same current as  $I_{R\_BC}$ .



Let's see if the current,  $I_{equiv}$ , is the same as  $I_{R\_BC}$ .

$$I_{equiv} = \frac{V_{in}}{R_{BC} / (1 + G)} = \frac{V_{in} (1 + G)}{R_{BC}} = V_{in} (1 + G) / R_{BC} = I_{R\_BC}$$

$$I_{equiv} = I_{R\_BC}$$

This confirms that the equivalent resistor referenced to ground is  $R_{BC} / (1 + G)$ .

This makes sense because it would take a smaller-value resistor referenced to ground with just  $V_{in}$  applied to it to drain the same amount of (higher) current that would have to be a resistor divided in value by  $(1 + G)$ . See [Figure 8-24](#).

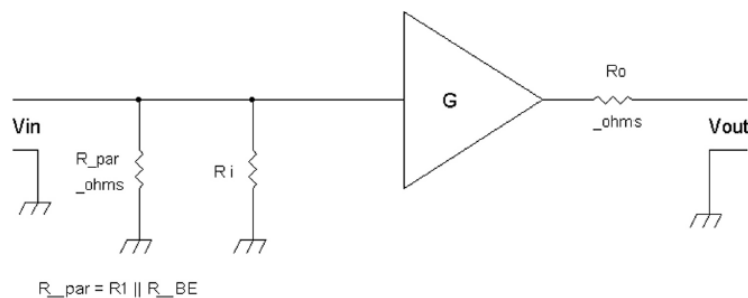
Note if the amplifier has no gain where  $G = 0$  that causes  $V_{out} = 0$  volt, then essentially  $R_{BC}$  is shorted to ground on the collector of  $Q_1$ , and we do indeed have  $R_{BC}$  as the equivalent resistor reference to ground.

$$R_{BC} / (1 + G)$$

with  $G = 0$

$$R_{BC} / (1 + 0) = R_{BC}$$

**Figure 8-24** AC model where  $R_i = [R_{BC} / (1 + G)] \parallel [R_{in \text{ base}}]$ .

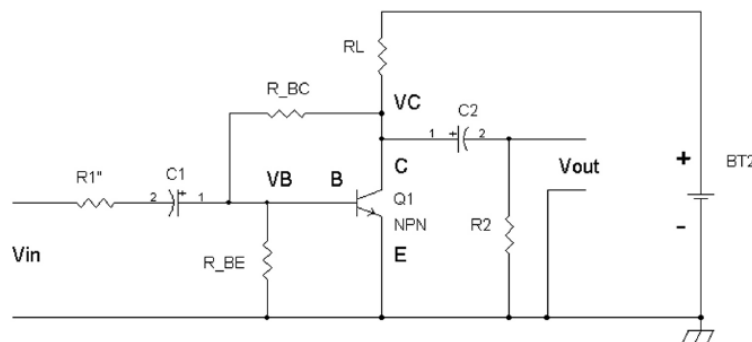


The output resistance,  $R_o$ , is actually dependent on the input signal's series source resistance. If  $V_{in}$  is driven by a pure voltage source or very low output impedance amplifier,  $R_o = R_L \parallel R_2 \parallel R_{BC}$ , which is similar to the simple amplifier in [Figures 8-3 and 8-7](#). Normally,  $R_{BC} \gg R_L \parallel R_2$ , so  $R_o \sim R_L \parallel R_2$ .

Because  $R_{BC}$  lowers the overall input resistance seen by  $V_{in}$  to almost "short" circuit compared to the other resistors,  $R_1$ ,  $R_{BE}$ , and  $R_{in}$  base, generally, we do not drive the input directly with a signal source with low source resistance.

However, we can improve upon the amplifier in [Figure 8-19](#) by adding a series resistor that will lower the gain,  $V_{out}/V_{in}$ , but then improves on raising the input resistance, lowering the output resistance, and also lowering the distortion for the same amplitude output. See [Figure 8-25](#).

**Figure 8-25** A modified one-transistor feedback amplifier with a series input resistor,  $R_1''$ .



We can define the gain  $G' = \frac{V_{out}}{V_B} = -(I_C/0.026 \text{ v}) \times (R_L \parallel R_{BC})$  that is relative to the signal voltage at the base of  $Q_1$ ,  $V_B$  and  $V_{out}$ , and not taking  $R_2$  into account for now.

And then we can define the actual gain  $\frac{V_{out}}{V_{in}} \sim -\frac{R_{BC}}{R_1''}$  where  $-\frac{R_{BC}}{R_1''} \leq 5\%$  of  $G'$ .

## 8.11. Output Resistance $R_o'$

The reader can skip over this section pertaining to the output resistance,  $R_o'$ , if desired. These calculations are long. The gist is having  $R_{BC}$  as a feedback resistor results in a lower output resistance than  $R_L \parallel R_2$ .

The output resistance,  $R_o'$ , not including  $R_2$  is approximately:

$$R_o' = \{[(R_{BC} + R_{in \text{ base}} \parallel R_{BE} \parallel R_1'')/(R_{in \text{ base}} \parallel R_{BE} \parallel R_1'')] \times (0.026 \text{ v}/I_C)\} \parallel R_L$$

Here are a couple of calculations with their measured results.

With  $BT_2 = 5$  volts,  $R_L = 2700\Omega$ ,  $R_{BC} = 100K\Omega$ ,  $R_{BE} = 40.2K\Omega$ , and  $R_1'' = 20K\Omega$ , the calculated gain  $(V_{out}/V_{in}) = -(R_{BC}/R_1'') = -100K/20K$ .

$$V_{out}/V_{in} = -5.0$$

Measured gain is  $-4.5$ , within 10 percent of the expected gain of  $-5$ .

Now let's calculate the output resistance, with  $R_2$  removed from the circuit in [Figure 8-25](#).

The calculated  $V_C \sim V_{BE} (1 + R_{BC}/R_{BE})$  where  $V_{BE} \sim 0.7 \text{ v}$ :

$$V_C \sim 0.7 \text{ v} (1 + 100K/40K) = 0.7 \text{ volt} (3.5)$$

$V_C \sim 2.45$  volts. The measured  $V_C$  was 2.3 volts.

With  $BT_2 = 5$  volts and  $V_C = 2.45$  volts with  $R_L = 2.7\text{K}\Omega$ , the calculated  $I_C \sim (BT_2 - V_C)/R_L$  since  $R_{BC} = 100\text{K}\Omega \gg R_L = 2.7\text{K}\Omega$ :

$$I_C \sim (5\text{ v} - 2.45\text{ v})/2.7\text{K}\Omega$$

$$I_C \sim 0.907\text{ mA}$$

The current gain  $\beta \sim 450$  for the 2N5089.

$$R_{in\text{ base}} = \beta (0.026\text{ v}/0.000907\text{ A}) = 450(286\Omega)$$

$$R_{in\text{ base}} = 12.9\text{K}\Omega$$

With  $R_{BC} = 100\text{K}\Omega$ ,  $R_{in\text{ base}} = 12.9\text{K}\Omega$ ,  $R_{BE} = 40.2\text{K}\Omega$ ,  $R_1'' = 20\text{K}\Omega$ , and  $R_L = 2700\Omega$

$$R_o' \sim \{[(R_{BC} + R_{in\text{ base}} \parallel R_{BE} \parallel R_1'') / (R_{in\text{ base}} \parallel R_{BE} \parallel R_1'')] \times (0.026\text{ v}/I_C)\} \parallel R_L$$

where  $R_{BC}$  in parallel with  $R_L$  is neglected since  $R_{BC} = 100\text{K}\Omega \gg R_L = 2.7\text{K}\Omega$ .

$$\text{Therefore: } R_o' \sim \{[(100\text{K}\Omega \parallel (12.9\text{K}\Omega \parallel 40.2\text{K}\Omega \parallel 20\text{K}\Omega)) / (12.9\text{K}\Omega \parallel 40.2\text{K}\Omega \parallel 20\text{K}\Omega)] \times (0.026\text{ v}/0.000907\text{ A})\} \parallel 2.7\text{K}\Omega$$

**Note:**  $(12.9\text{K}\Omega \parallel 40.2\text{K}\Omega \parallel 20\text{K}\Omega) = 6.56\text{K}\Omega$ .

$$R_o' \sim \{[(100\text{K}\Omega + 6.56\text{K}\Omega)/(6.56\text{K}\Omega)] \times (0.026\text{ v}/0.000907\text{ A})\} \parallel 2.7\text{K}\Omega$$

$$R_o' \sim \{16.24 \times (0.026\text{ v}/0.000907\text{ A})\} \parallel 2.7\text{K}\Omega$$

$$R_o' \sim \{16.24 \times (28.66\Omega)\} \parallel 2.7\text{K}\Omega$$

$$R_o' \sim 465\Omega \parallel 2.7\text{K}\Omega$$

$$R_o' \sim 465\Omega \parallel 2.7\text{K}\Omega$$

$$R_o' \sim 397\Omega \text{ calculated}$$

$R_o' \sim 390\Omega$  measured via setting  $R_2 = 390\Omega$  and noticing that the signal dropped by 50 percent.

The output resistance,  $R_o'$ , calculation is rather long, and sometimes we do not have time to do this. Here are some rules of thumb concerning the transistor amplifier.

1. Use low-value gains that are typically less than  $\beta$  or 10, such that  $R_{BC}/R_1'' \leq 10$ .
2. Make sure that  $R_{BC} \gg R_L$  by at least tenfold. Thus,  $R_{BC}$  does not lower the gain  $G$  by much since as "seen" by the collector of  $Q_1$ ,  $R_L$  and  $R_{BC}$  are essentially in parallel. The reason is that the resistors  $R_{BE}$  and  $R_{in\text{ base}}$  that are coupled to ground and connected to  $R_{BC}$  at the base are  $\ll R_{BC}$ , that is  $(R_{BE} \parallel R_{in\text{ base}}) \ll R_{BC}$ .
3. Bias the DC voltage at the collector,  $V_C$ , to be at one-half the power supply voltage.
4. Use as high  $\beta$  transistor as you can, such as a 2N5089. If you use a lower  $\beta$  transistor such as a general-purpose type, 2N3904, then you may have to set for lower gains such as  $R_{BC}/R_1'' \leq 5$ .
5. Generally, bias the collector current,  $I_C$ , in the range of 0.2 mA to  $\beta$  mA with the appropriate value  $R_L$  resistor that is scaled from the example at  $\sim 1$  mA where  $R_L = 2700\Omega$ . For instance, if you are running  $I_C$  at 200  $\mu\text{A}$ , then  $R_L \sim \beta \times 2700\Omega$  or about 12K $\Omega$ , and  $R_{BC} \sim \beta \times 100\text{K}\Omega = 510\text{K}\Omega$ ,  $R_{BE} \sim \beta \times 40.2\text{K}\Omega = 200\text{K}\Omega$ , and  $R_1'' = 100\text{K}\Omega$ . Going the other direction with  $I_C = 5$  mA, all the resistors that were used for  $I_C \sim 1$  mA are scaled by (1/5) or 20 percent or 0.2. Thus,  $R_L \sim 0.2 \times 2700\Omega \sim 560\Omega$ ,  $R_{BC} \sim 0.2 \times 100\text{K}\Omega \sim 20\text{K}\Omega$ ,  $R_{BE} \sim 0.2 \times 40.2\text{K}\Omega = 8.2\text{K}\Omega$ ,  $R_1'' \sim 0.2 \times 20\text{K}\Omega \sim 3.9\text{K}\Omega$ .

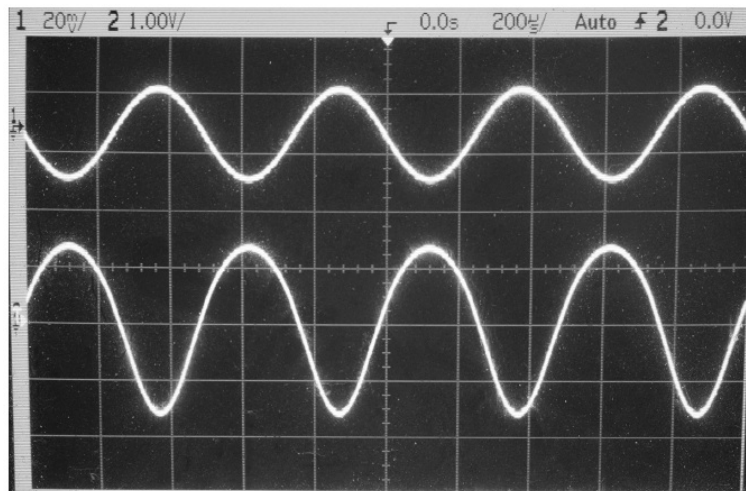
Note the input capacitor,  $C_1$ , can be scaled according to the collector currents. For example, if a 1  $\mu\text{F}$  is used for 1 mA collector, then 4.7  $\mu\text{F}$  is used for  $\beta$  mA  $I_C$ , and 0.22  $\mu\text{F}$  is used for 0.2 mA collector current. However for  $C_1$ , you can always just use the highest value capacitor for all cases such as 4.7  $\mu\text{F}$  or greater capacitance. The output capacitor  $C_2$  should be greater than or equal to 4.7  $\mu\text{F}$  to ensure good low frequency response.

6. One feature of this amplifier is that the performance increases as you set the gain lower via lower ratios of  $R_{BC}$  to  $R_1$ . This is normally done by increasing the value of  $R_1$ . The increase in performance parameters result in lower output resistance,  $R_o$ , and lower harmonic distortion at  $V_{out}$  for the same output amplitude.
7. Another feature of this amplifier is that you can set the inverting gain to attenuate the signal. That is,  $0 < |R_{BC}/R_1| < 1$ . For example, if  $R_{BC} = 100\text{K}\Omega$ , we can set  $R_1 = 300\text{K}\Omega$  for a gain of  $- (1/3)$  or  $- 0.33$ . This can be useful if the amplifier is interfacing with a signal source whose amplitude exceeds the amplifier's power supply voltage,  $BT_2$ . For example if your generator or signal source provides 10 volts peak to peak, and your amplifier can only deliver about 4 volts peak to peak, having the gain set to  $-0.33$  will keep the output from clipping since the output voltage will be 10 volts  $\times (-0.33)$  peak to peak or 3.3 volts peak to peak.

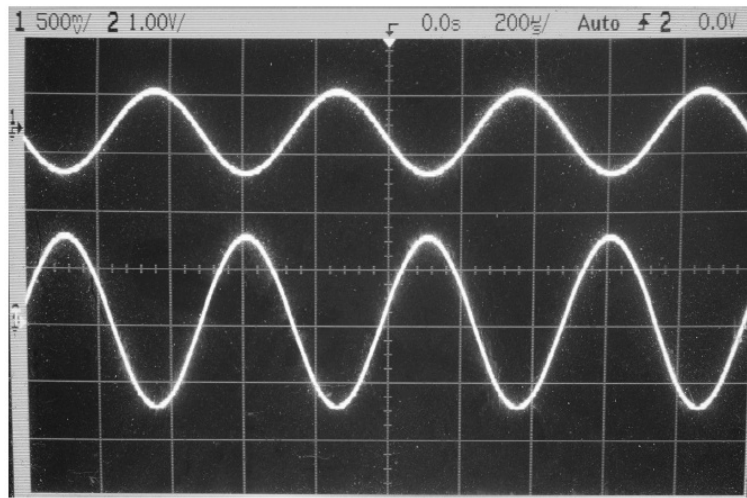
Referring to #6, see [Figure 8-26](#), which shows the output waveform for the circuit in [Figure 8-25](#), where the gain is  $\sim -94$  via input series resistor  $R_1 = 25\Omega$ . In comparison see [Figure 8-27](#) where the distortion is lower for the same output voltage because  $R_1$  is increased to  $20\text{K}\Omega$  for a (lower) gain of  $- 4.2$ .

To lower output signal distortion  $R_1$  is increased to  $20\text{k}\Omega$ . See [Figure 8-27](#) bottom trace.

**Figure 8-26**  $R_1 = 25\Omega$ ,  $V_{in} = 32\text{ mV}$  peak to peak (top waveform), and bottom waveform  $V_{out} = 3\text{ v}$  peak to peak with 12 percent harmonic distortion. Gain  $\sim -94 = V_{out}/V_{in}$ . Also note the phase inversion between the output signal  $V_{out}$  and the input signal  $V_{in}$ .



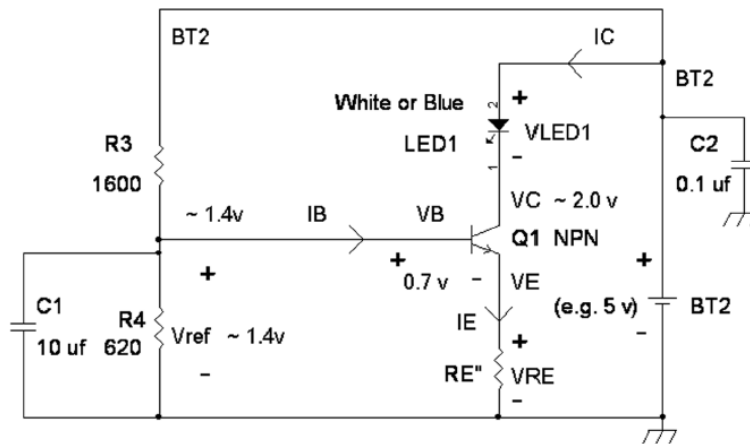
**Figure 8-27**  $R1 = 20K\Omega$ ,  $V_{in} = 720\text{ mV}$  peak to peak (top trace), and  $V_{out} = 3\text{ v}$  peak to peak for a gain of  $-4.2$  (bottom trace). Harmonic distortion measured at 1 percent. Again, note the phase inversion of  $V_{out}$  with respect to  $V_{in}$ .



## 8.12. Another Common Emitter Amplifier

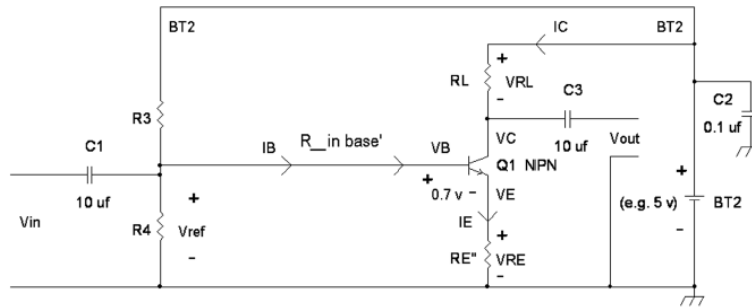
We will now look at another type of common emitter amplifier with a series emitter resistor derived from an LED drive circuit. See [Figure 8-28](#), which shows a constant current source LED drive circuit, and then [Figure 8-29](#), which converts the LED drive circuit into an amplifier.

**Figure 8-28** A constant current source amplifier where the LED drive current  $= V_E/RE$ .



We can reconfigure the constant current source circuit to an amplifier by replacing the LED with a load resistor,  $R_L$ , and coupling an input signal voltage to the base with a capacitor. See [Figure 8-29](#).

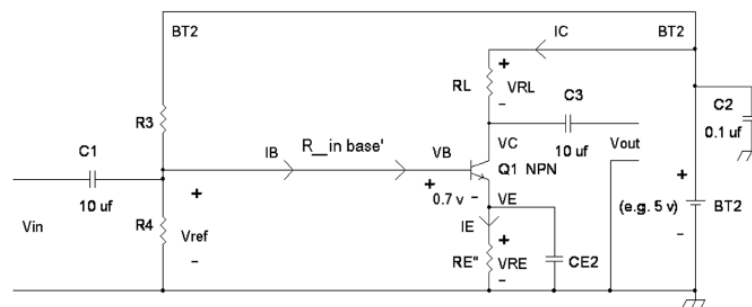
**Figure 8-29** A simple common emitter amplifier with a series emitter resistor  $R_E$ .



To bias this correctly, generally " $V_{ref} = BT2[R4/(R3 + R4)]$ " is less than half the supply but  $\geq 0.5$  volts. Typical collector currents can range from 50  $\mu A$  to about 20 mA for a small signal transistor such as the 2N3904. Generally, the voltage divider resistors  $\geq 470\Omega$ , and the emitter resistor  $R_E$  that sets the DC collector current can be anywhere from about  $100\Omega$  to  $10K\Omega$ . Collector current  $I_C = V_E/R_E$ , where  $\beta \gg 1$ , which is usually the case. In terms of gain, a first approximation has  $V_{out}/V_{in} \sim -R_L/(r_e + R_E)$ , where  $r_e = (0.026 \text{ v})/I_C$ . Again, this is an inverting amplifier. Generally, it's harder to provide very high gains from this configuration unless very high supply voltages are used. For example, if we want a gain of  $-100$ , and  $I_C = 1 \text{ mA}$ , with  $V_E = 1 \text{ volt}$  and  $R_E = 1000\Omega$ , then  $R_L$  has to be  $\sim 100K\Omega$ . This would require  $BT2 > 100$  volts. For example,  $BT2 = 200$  volts so that  $V_C$  is operating at 100 volts DC. Also, a general-purpose transistor will have insufficient breakdown voltage and a high-voltage transistor such as a 2N3439 or MPSA42 would be used instead. If we want instead a gain  $\sim -10$ , then we can have  $R_L = 10K\Omega$ ,  $BT2 = 20$  volts,  $Q1 = 2N3904$ , with  $V_C \sim 10$  volts when  $I_C = 1 \text{ mA}$ .

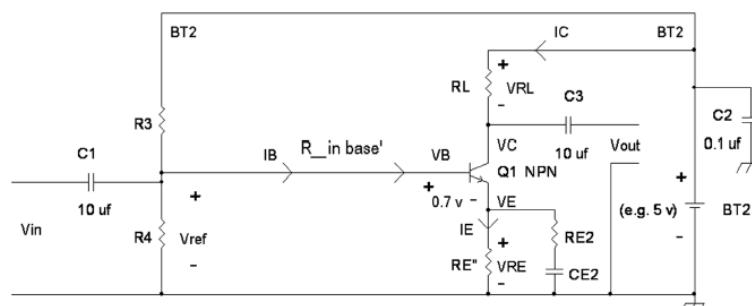
An emitter bypass capacitor CE2 provides higher gain ( $V_{out}/V_{in}$ ) at the expense of higher distortion. But this circuit allows for lower supply voltages. See [Figure 8-30](#).

**Figure 8-30** Capacitor CE2 effectively AC grounds Q1's emitter.



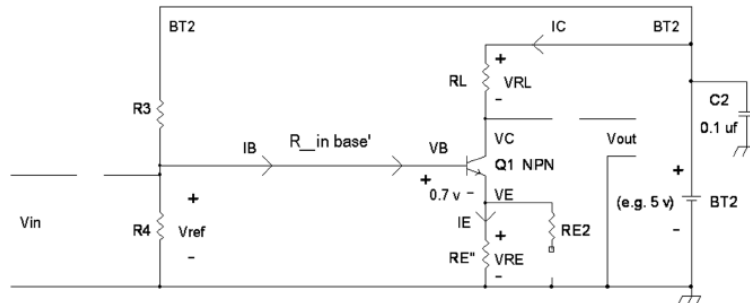
By adding a resistor (RE2) in series with capacitor CE2, the AC gain can be set without upsetting Q1's DC bias points (e.g., VB and IC). See [Figure 8-31](#), which includes RE2.

**Figure 8-31** A second series emitter resistor,  $RE2$ , allows for increasing the gain without changing the DC bias conditions. Capacitor  $CE2$  has a large capacitance such that it is an AC short circuit.



In [Figure 8-31](#), with RE2 in series with CE2, the gain  $G = -[R_L / (r_e \parallel R_E'' \parallel R_{E2})]$ , where  $r_e = (0.026 \text{ V} / I_C)$ . To find the DC operating points, VC, IC, and VE, we remove the capacitors as shown in [Figure 8-32](#).

**Figure 8-32** A DC analysis circuit of [Figure 8-31](#) where capacitors are removed.



With the capacitors removed and neglecting DC base currents due to IB,  $V_B \sim BT2 [R4 / (R3 \parallel R4)]$  and with Q1's turn-on voltage,  $V_{BE} \sim 0.7 \text{ V}$  DC,  $V_E \sim V_B - 0.7 \text{ V}$ . The collector current  $I_C \sim I_E$ , the emitter current when  $\beta \gg 1$ , which is usually the case. We now have:

$$I_E = V_E / R_E''$$

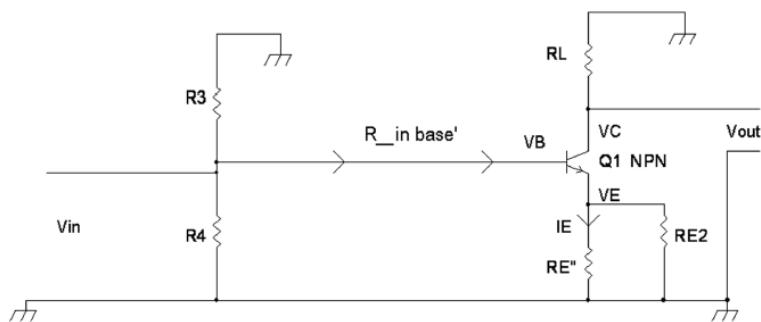
$$I_C \sim V_E / R_E''$$

We now have to also find AC resistance,  $R_{in \text{ base'}}$ , which can be found via  $I_C$ ,  $\beta$ ,  $r_e$ ,  $R_E''$ , and  $R_{E2}$ .

$$R_{in \text{ base}} = \beta r_e \parallel (\beta + 1) (R_E'' \parallel R_{E2}), \text{ where } r_e = (0.26 \text{ V} / I_C).$$

For the AC analysis model, see [Figure 8-33](#).

**Figure 8-33** An AC signal analysis circuit.



For example, if  $BT2 = 6 \text{ V}$ ,  $R3 = 40.2 \text{ K}\Omega$ ,  $R4 = 20 \text{ K}\Omega$ ,  $R_E'' = 3900 \Omega$ ,  $R_L = 10 \text{ K}\Omega$ ,  $R_{E2} = 1 \text{ K}\Omega$ ,  $\beta = 150$ , then  $V_B \sim 6 \text{ V} (20 \text{ K} / (40.2 \text{ K} + 20 \text{ K})) \sim 6 \text{ V} (20 / 60.2 \text{ K})$   $V_B \sim 2 \text{ V}$ .

$V_E \sim V_B - 0.7 \text{ V} = (2 - 0.7) \text{ V}$  or  $V_E = 1.3 \text{ V}$ .  $I_C \sim V_E / R_E'' = 1.3 \text{ V} / 3900 \Omega$  or  $I_C \sim 0.00033 \text{ A}$ .

To find the gain, G, we calculate for:

$$r_e = (0.026 \text{ V}/I_C) = (0.026 \text{ V})/(0.00033 \text{ A}) \text{ or } r_e = 78.8\Omega$$

$$G = -[R_L/(r_e + R_{E''} \parallel R_{E2})]$$

$$R_{E''} \parallel R_{E2} = 3900\Omega \parallel 1\text{K}\Omega = 796\Omega, \text{ thus}$$

$$G = -[10\text{K}/(78.8 + 796)] \text{ or } G \sim -11.4, \text{ and with } \beta = 150 \text{ we have:}$$

$$R_{in \text{ base}} = \beta r_e + (\beta + 1) (R_{E''} \parallel R_{E2}) = 150 (78.8\Omega) + (150 + 1) (796\Omega)$$

$$R_{in \text{ base}} \sim (11.82\text{K}\Omega + 120.2\text{K}\Omega)$$

$$R_{in \text{ base}} = 132.02\text{K}\Omega$$

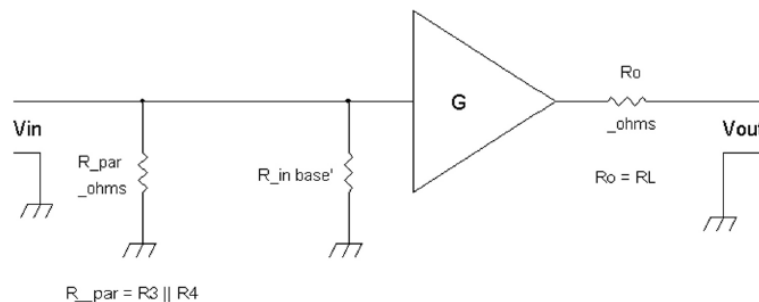
When  $R_{E''} \parallel R_{E2} \gg r_e$ , the emitter resistors  $R_{E''}$  and  $R_{E2}$  are the main contributors for  $R_{in \text{ base}}$  that leads to:  $R_{in \text{ base}} \sim (\beta + 1) (R_{E''} \parallel R_{E2})$ .

From [Figure 8-34](#), to find the AC input resistance to the amplifier, it is  $(R_{\text{par}} \parallel R_{in \text{ base}}')$ , where  $R_{\text{par}} = R_3 \parallel R_4$ . With the example where  $R_3 = 40.2\text{K}\Omega$ ,  $R_4 = 20\text{K}\Omega$ , and the calculated  $R_{in \text{ base}}' = 132.02\text{K}\Omega$ , the input resistance is:

$$R_3 \parallel R_4 \parallel R_{in \text{ base}}' = (40.2\text{K}\Omega \parallel 20\text{K}\Omega) \parallel 132.02\text{K}\Omega = (13.33\text{K}\Omega) \parallel 132.02\text{K}\Omega$$

$$R_3 \parallel R_4 \parallel R_{in \text{ base}}' = 12.13\text{K}\Omega$$

**Figure 8-34** AC signal analysis block diagram with output resistance  $R_o = R_L$ .



The input resistance =  $12.13\text{K}\Omega$ .

We can reiterate the gain calculation for  $G$  from knowing the collector current and the values of the collector resistor  $R_L$  and emitter resistors,  $R_{E''}$  and  $R_{E2}$  along with  $r_e$ .

$$G = -[R_L/(r_e + R_{E''} \parallel R_{E2})]$$

$$r_e = 78.8\Omega = (0.026 \text{ V}/I_C), \text{ where } I_C = 0.00033 \text{ A as calculated previously.}$$

$$R_{E''} \parallel R_{E2} = 3900\Omega \parallel 1\text{K}\Omega = 796\Omega, R_L = 10\text{K}\Omega \text{ and thus } G = -[10\text{K}/(78.8 + 796)]$$

$$G \sim -11.4$$

The output resistance,  $R_o = R_L$ , and with  $R_L = 10\text{K}\Omega$  in this example,  $R_o = 10\text{K}\Omega$ .

**NOTE:** An amplifier having a high output resistance such as  $10\text{K}\Omega$  results in a gain reduction of  $G$  when driving a subsequent device (e.g., input stage of another amplifier). If  $V_{out}$  is loading into another device that has an effective  $10\text{K}\Omega$  to ground will cause the gain,  $G$ , drop from  $-11.4$  to half or  $G \rightarrow -5.7$ .

Typical input resistances of audio power amplifiers are between  $1\text{K}\Omega$  to  $100\text{K}\Omega$ .

For example, an amplified computer stereo loudspeaker with a 3.5 mm connector has a typical input resistance of  $10\text{K}\Omega$ .

## 8.12.1. Troubleshooting the Amplifier in [Figure 8-31](#)

1. For measuring the DC conditions, turn off the AC signal source and measure the collector, base, and emitter DC voltages, VC, VB, and VE. Make sure that the transistor is in the amplifying region (forward active region) and not in the saturation region. This can be confirmed by measuring with a DVM that the voltage across the collector and emitter (VCE) > 11 volt DC, or that the collector to base (VCB) voltage > 0.7 volt. Generally, we should expect that VCE or VCB is in the range of at least a quarter of power supply voltage. For example, if BT2 = 12 volts, then  $V_{CE} \geq 3$  volts. In another example, if BT2 = 5 volts, then the DC voltages across the collector to base (VCB) and across the collector to emitter (VCE) should be  $\geq 25$  percent (5 volts) or  $\geq 1.25$  volts.
2. Confirm that R3, R4, RE", and RL are correct. Measure the resistors with the power turned off and with one lead of each resistor disconnected from the circuit. In a special case, you can measure RE2 in circuit because it has a series DC blocking capacitor CE2, but you may have to keep the ohm-meter's probes across RE2 for about 10 seconds to let the resistance measurement settle.
3. With power turned back on, confirm that the voltages comply with the expected voltage from the voltage divider circuit with R3 and R4. That is,  $V_B = BT2[R4/(R3 + R4)]$ , and  $V_E = V_B - 0.7$  volt.
4. Confirm that the emitter current is approximately equal to the collector current by measuring the voltage across RL = VRL and voltage across RE" = VRE. Then confirm via calculation from the resistance values of RL and RE" and the measured voltages, VRL and VRE that  $V_{RL}/R_L \sim V_{RE}/R_E$  is within 15 percent if = percent resistors are used.
5. If the DC voltages seem unstable, the amplifier may be oscillating at >100MHz. Try inserting a 100Ω series base resistor close to Q1 and see if the DC voltages stabilize and measure to their expected values.
6. With the signal generator turned on having a small amplitude such as 100 mV peak to peak at Vin, measure the AC signal at VE with an **oscilloscope**. The AC signal at VE should be approximately 100 mV peak to peak within about 25 percent on the low side (e.g., VE's output AC voltage is in the range of 75 mV to 100 mV peak to peak). Note that the AC voltage at the emitter is the same phase as the base since the emitter terminal acts like having a 0.7 volt DC source voltage between the base and the emitter. **A DC voltage source such as the VBE turn-on voltage in series with an AC signal source at the base cannot change the phase of the AC signal at the emitter.** The output signal at the collector, VC, should be  $G \times 100$  mV peak to peak, or in this example, where  $G = -11.4$ , Vout AC should be about 1.14 volts peak to peak that is out of phase with the input signal at the base.
7. In [Figures 8-30](#) and [8-31](#) emitter capacitors CE and CE2 are chosen to determine the low-frequency response. The 10 μf input and output capacitors, C1 and C3, are designed with sufficient capacitance for most applications with a 20 Hz or lower cut-off frequency. For example, for audio applications, where a low-frequency response of  $\leq 20$ Hz is required, C1 and C3 generally will work because input and output resistances are generally greater than 1KΩ.

For example, the cut-off frequency with a 10 μf capacitor and 1KΩ resistor is:

$$1/[2\pi 10 \mu f (1K\Omega)] \sim 16 \text{ Hz}$$

To determine the worst-case capacitance values for CE and CE2, choose the low-end frequency you want such as 20Hz. Then use the following formula:

$$C_E \text{ or } C_{E2} = 1/[2\pi f_c r_e]$$

Let  $f_c = 20 \text{ Hz}$  = low-frequency cut-off frequency for an audio application that responds to bass note frequencies.

For example, if  $I_C = 1 \text{ mA}$ , then  $r_e = (0.026 \text{ V}/0.001\text{A})$  or  $r_e = 26\Omega$ .

$$C_E \text{ or } C_{E2} = 1/[2\pi 20\text{Hz } 26\Omega] = 3.06 \times 10^{-4} \text{ Farad or } 306 \mu f$$

The closest commercially available value is 330  $\mu\text{f}$ , but to ensure a safety margin just in case, use a 470  $\mu\text{f}$  unit if possible. Since the emitter voltage is generally less than 25 volts, you can use at least a 16-volt electrolytic capacitor. Make sure the (-) terminal of CE or CE2 is grounded.

8. Confirm that any electrolytic capacitors in the circuit are correctly connected (polarity-wise) to avoid reverse biasing. Reverse biasing electrolytic capacitors usually cause the DC bias points to be wrong, due to current leakage through the electrolytic capacitors.
9. The common emitter amplifier in [Figure 8-30](#) where capacitor CE is an AC short circuit from emitter to ground has the same input amplitude limitation as the simple bias circuit in [Figure 8-11](#) for tolerable distortion at the output,  $V_{\text{out}}$ . By tolerable distortion, an example would be for intelligible voice signals, < 10 percent harmonic distortion is workable. That is, generally the input signal,  $V_{\text{in}}$ , is limited to less than 10 mV or 20 mV peak to peak when driven by a low impedance source signal such as a 50 $\Omega$  generator. If  $V_{\text{in}}$  is driven with a larger value source resistance such as a  $\geq 10\text{K}\Omega$  series resistor, the distortion will be lower but the voltage gain will be lower as well due to the input resistance forming a voltage divider circuit.

For higher-fidelity applications that require lower distortion at the output less than 1 percent, use the circuit in [Figure 8-31](#). See #10 below concerning distortion calculations.

10. In [Figure 8-31](#) where CE2 is an AC short circuit (e.g., CE = 470  $\mu\text{f}$ ), we can estimate the input signal's amplitude for second order harmonic distortion at the output. Note that  $V_{\text{in\_mV\_peak}}$  is measured in peak amplitude sinewave.

$$\text{Harmonic distortion in percent} = (V_{\text{in\_mV\_peak}} \left[ \frac{1}{1 + (R_E'' \parallel R_{E2}/r_e)} \right]^2) \%$$

Where  $r_e = r_e = (0.026 \text{ v}/I_C)$ .

For example, for [Figure 8-31](#):

$B_T2 = 6 \text{ volts}$ ,  $R_3 = 40.2\text{K}\Omega$ ,  $R_4 = 20\text{K}\Omega$ ,  $R_E'' = 3900\Omega$ ,  $R_L = 10\text{K}\Omega$ ,

$R_{E2} = 1\text{K}\Omega$ ,  $G = -11.4$

$r_e = (0.026 \text{ v}/I_C) = (0.026 \text{ v})/(0.00033\text{A})$  or  $r_e = 78.8\Omega$

$R_E'' \parallel R_{E2} = 3900\Omega \parallel 1\text{K}\Omega = 796\Omega$

$(R_E'' \parallel R_{E2}/r_e) = 796/78.8 \sim 10$

$1 + (R_E'' \parallel R_{E2}/r_e) = 1 + 10 = 11$

Second order harmonic distortion in percent =

$$(V_{\text{in\_mV\_peak}} \left[ \frac{1}{1 + (R_E'' \parallel R_{E2}/r_e)} \right]^2) \%$$

$$\text{Second order harmonic distortion in percent} = (V_{\text{in\_mV\_peak}} \left[ \frac{1}{11} \right]^2) \%$$

$$\text{Second order harmonic distortion in percent} = (V_{\text{in\_mV\_peak}} \times \frac{1}{121}) \%$$

So, if  $V_{\text{in}} = 121 \text{ mV peakpeak}$  (which is also 242 mV peak to peak), then:

$$\text{Second order harmonic distortion in percent} = (121 \times \frac{1}{121}) \% = 1\%$$

$V_{\text{in}}$ 's peak to peak voltage for 1 percent second order distortion is then  $2 \times 121 \text{ mV peak to peak}$  or 242 mV peak to peak. This 242 mV peak to peak input level assumes that the output has not clipped. With a gain  $G = -11.4$ , the output will be  $V_{\text{out}} = 2.76 \text{ volts peak to peak}$  ( $11.4 \times 242 \text{ mV p-p}$ ).

Note that the 2nd order harmonic distortion formula is proportion to input level. That is doubling the signal level results in twice the distortion, or halving the input level gives half the distortion at the output.

A safer estimate to ensure that there is no clipping is to reduce  $V_{in}$  to the 0.5 percent level. This is just one half of 242 mV peak to peak input level for 121 mV peak to peak that results in the output.

$V_{out} = 1.36$  volts peak to peak for 0.5 percent second harmonic distortion

## 8.13. Maximum Output Voltage Swing

We will now examine how to achieve maximum output swing in differently configured common emitter amplifiers.

### 8.13.1. Amplifier's Emitter AC Grounded via CE

The DC collector voltage will determine output voltage swing. For the circuit in [Figure 8-30](#), where capacitor CE is an AC short circuit, the maximum voltage swing will be from  $V_E$  to  $BT_2$ . For example, if  $V_B$  is 2 volts, then  $V_E = 1.3$  volts due to the 0.7-volt base – emitter voltage. If  $BT_2 = 6$  volts, then the peak to peak output swing will be from 11.3 volts to 16 volts, which will be (6 volts – 1.3 volts) peak to peak or 4.7 volts peak to peak. However, often the DC collector voltage is not centered to give maximum voltage swing without clipping prematurely on one-half of a sine wave cycle before the other half of the sine-wave. To maximize, you can set the DC collector voltage at the average of  $BT_2$  and  $V_E$ , which is  $V_C = (BT_2 + V_E)/2$ .

For this example:

$V_C = (6 \text{ volts} + 1.3 \text{ volts})/2$  or  $V_C = 3.65$  volts for “symmetrical” clipping

### 8.13.2. Amplifier's Emitter Partially AC Grounded via Series RE2 and CE2

In [Figure 8-31](#), we have a little bit more going on because both emitter and collector terminals have AC output signals. Clipping occurs when either the collector voltage approaches the power supply voltage (e.g.,  $BT_2$ ), or when the collector voltage matches the (same) voltage at the emitter. That is during the positive sine-wave cycle of the emitter and the negative cycle of the collector matches the voltage across the collector and emitter (e.g.,  $V_{CE}$ ) is approximately 0 volt. Put in other words, the collector voltage equals (or matches) the emitter voltage.

For [Figure 8-31](#) where  $RE_2$  is generally  $> r_e$ , the input signal range for “undistorted” output can be approximated when  $RE \parallel RE_2 \gg r_e$  as follows: Turn off the input signal and measure DC voltages for  $V_C$  and  $V_E$ . Let's call these DC voltages,  $V_{C_{dc}}$  and  $V_{E_{dc}}$ . The total collector voltage swinging downward toward the emitter's voltage is  $V_{C_{dc1ac}} = V_{C_{dc}} + G V_{in_{peak}}$  and the total voltage at the emitter swinging up toward the collector voltage is  $V_{E_{dc1ac}} \sim V_{E_{dc}} + V_{in_{peak}}$ .

The input voltage that can be found by the collector voltage equals the emitter voltage:

$$V_{C_{dc+ac}} = V_{E_{dc+ac}}$$

$$V_{C_{dc}} + G V_{in_{peak}} = V_{E_{dc}} + V_{in_{peak}}$$

To find  $V_{in_{peak}}$ , this can be summarized as:

$$V_{in_{peak}} = (V_{C_{dc}} - V_{E_{dc}})/(1 - G)$$

A step-by-step calculation is now shown.

For example,  $BT_2 = 6$  volts,  $R_L = 10\text{K}\Omega$ ,  $R_3 = 40.2\text{K}\Omega$ ,  $R_4 = 20\text{K}\Omega$  so  $V_B = BT_2 [R_4/(R_3 + R_4)] = 6$  volts  $[20\text{K}/(40.2\text{K} + 20\text{K})] = 6$  volts  $[20\text{K}/60.2\text{K}]$   $V_B \sim 6$  volts  $[2/6]$  or  $V_B \sim 2$  volts.  $I_C \sim V_E/R_E = (V_B - 0.7 \text{ volt})/3900\Omega$  or  $I_C \sim 1.3 \text{ v}/3900\Omega$  or  $I_C = 0.00033 \text{ A}$ . This makes  $V_{C_{dc}} = 6$  volts  $- I_C(R_L)$  or:

$$V_{C_{dc}} = 2.7 \text{ volts. } V_{E_{dc}} = V_B - 0.7 \text{ volts} = 2 \text{ volts} - 0.7 \text{ volt} = 1.3 \text{ volts}$$

$$V_{E_{dc}} = 1.3 \text{ volts}$$

We need to equate  $V_{C_{dc1ac}} = V_{E_{dc1ac}}$  to find the maximum peak voltage swing at clipping.

$$V_{C_{dc}} + G V_{in_{peak}} = V_{E_{dc}} + V_{in_{peak}}$$

$V_{C_{dc}} - V_{E_{dc}} = G V_{in_{peak}} - V_{in_{peak}} = (1 - G) V_{in_{peak}} = (V_{C_{dc}} - V_{E_{dc}})$  or  $V_{in_{peak}} = (V_{C_{dc}} - V_{E_{dc}})/(1 - G)$ , to get a positive value in terms of peak input voltage:

$$V_{in_{peak}} = (V_{C_{dc}} - V_{E_{dc}})/(1 - G)$$

For this example:

$$V_{C_{dc}} = 2.7 \text{ volts}$$

$$V_{E_{dc}} = 1.3 \text{ volts}$$

$$G = -11.4$$

$$V_{in_{peak}} = (V_{C_{dc}} - V_{E_{dc}})/(1 - G)$$

$$V_{in_{peak}} = (2.7 \text{ v} - 1.3 \text{ v})/(1 - (-11.4)) = 1.4 \text{ v}/(12.4)$$

$$V_{in_{peak}} = 0.1129\text{-volt peak input}$$

The output peak voltage:

$$V_{out_{peak}} = V_{in_{peak}} \times |G|$$

$$G = -11.4 \rightarrow |G| = 11.4$$

$$V_{out_{peak}} = 0.1129\text{-volt peak} \times 11.4$$

$$V_{out_{peak}} = 1.287 \text{ volts peak}$$

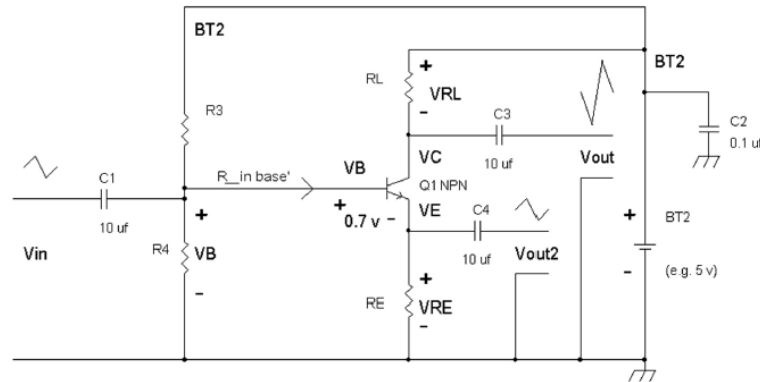
$$V_{out_{peak \text{ to peak}}} = 2.574 \text{ volts peak to peak}$$

In practice both  $V_{in_{peak}}$  and  $V_{out_{peak}}$  will be slightly smaller to avoid clipping or distortion.

## 8.14. Finding an Optimum Bias Point for Maximum Output Swing with Just an Emitter Resistor

With a common emitter amplifier with just a series emitter resistor (e.g.,  $R_E$ ) and where the series emitter resistor  $\gg \frac{1}{\beta} = (0.026 \text{ v}/I_C)$ , we can find an optimal bias voltage based on the collector load resistor,  $R_L$  and series emitter resistor,  $R_E$ . See [Figure 8-35](#).

**Figure 8-35** A common emitter amplifier with an emitter series resistor,  $R_E$ .



To find an optimal biasing voltage,  $V_B$ , given the values for  $R_L$  and  $R_E$ , we have:

$$V_B = \frac{BT2}{2} \frac{1}{1 + \frac{R_L}{R_E}} + 0.7 \text{ volt}$$

For example if we want to make a unity gain phase splitter amplifier where amplitudes of the AC signals are about equal via the collector and emitter terminals ( $V_{out}$  and  $V_{out2}$ ),  $R_L = R_E$ .

**NOTE:** For a phase splitter amplifier circuit, output terminals  $V_{out}$  and  $V_{out2}$  are generally loaded with equal resistance values of at least  $10 \times R_L$ .

If  $BT2 = 12$  volts, and  $R_L = R_E = 1K\Omega$ , then:

$$V_B = \frac{12v}{2} \frac{1}{1 + \frac{1K}{1K}} + 0.7 v = 6 v \times \frac{1}{2} + 0.7 v$$

$$V_B = 3 v + 0.7 v \text{ or } V_B = 3.7 \text{ volts}$$

This would mean  $V_E = V_B - 0.7 v$  or  $V_E = 3$  volts.

If there is a 3-volt drop across  $R_E$ , then there should be a 3-volt drop across  $R_L$  since  $R_E = R_L$ , given that the emitter current = collector current for  $\beta \gg 1$ . That is  $V_{RL} = V_{RE}$ .

Thus,  $V_C = BT2 - V_{RL} = BT2 - V_{RE} = 12 v - 3 v$  or  $V_C = 9$  volts.

This makes sense because at  $V_E = 3$  volts, the maximum swing at the emitter is  $3 \text{ volts} \pm 3 \text{ volts}$  or 0 volt to 6 volts at the emitter. If there is 6 volts at the emitter for  $V_E$ , then the collector voltage is  $V_C = BT2 - V_{RE} = 12 v - 6 v$ , or  $V_C = 6$  volts. This then satisfies the condition that maximum swing is when the collector and emitter voltages are equal.

In practice the collector-to-emitter voltage is rarely 0 volt but close, such as 0.2 volt. And this will reduce the maximum calculated swing by a slight amount. But this equation is fine for a first approximation.

$$V_B = \frac{BT2}{2} \frac{1}{1 + \frac{R_L}{R_E}} + 0.7 \text{ volt}$$

With  $R_L = R_E = 1K\Omega$ , and  $BT2 = 12$  volts, here are example resistor values for  $R_3 = 39K\Omega$  and  $R_4 = 18K\Omega$ . And we can confirm that  $V_B$  is close to 3.7 volts.

$$V_B = 12 \text{ v} [R_4 / (R_3 + R_4)] = 12 \text{ v} [18\text{K} / (39\text{K} + 18\text{K})] = 12 \text{ v} [18\text{K} / 57\text{K}]$$

$$V_B = 12 \text{ v} [0.3158] \text{ or}$$

$$V_B = 3.789 \text{ volts} \sim 3.7 \text{ volts}$$

Because  $R_E = 1\text{K}\Omega$  and  $R_3 \parallel R_4 < 20R_E \rightarrow 39\text{K}\Omega \parallel 18\text{K}\Omega < 20\text{K}\Omega = 20R_E$ , we can use a transistor of  $\beta \geq 100$  such as a 2N3904.

## 8.15. Summary

The amplifiers presented have limitations in terms of input amplitudes and output swing. Distortion can be a problem unless there is a series input resistor or a series emitter resistor that reduces gain and distortion. Be aware of the capacitors' capacitance values at the input, at the output, and especially connected to the emitter (e.g.,  $C_E$  and  $C_{E2}$ ), which will determine the amplifier's low-frequency performance.

Also, make sure electrolytic capacitors are biased correctly; otherwise, they will be reverse biased. Having electrolytic capacitors wired backwards results in leakage currents that will cause the expected DC bias points to shift up or down. You can use a voltmeter to confirm the correct polarity voltage across the electrolytic capacitors.

This concludes Chapter 8 concerning simple one-transistor amplifiers. In [Chapter 9](#) we will explore some linear integrated circuits such as operational amplifiers and voltage regulators.